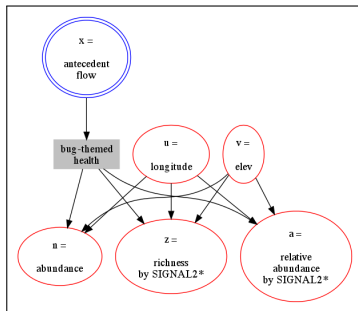


LHFI: statistical model-based inference for stream health



Grace S Chiu^{1,2,3,4,5}

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1. Conventional vs LHFI

Average 2000-2010 Stream Health in Chesapeake Bay Sub-watersheds

Chesapeake Bay Program
A Watershed Partnership

Average Benthic Index of Biotic Integrity Rating

- Excellent
- Good
- Fair
- Poor
- Very Poor
- No Score
- Chesapeake Bay Watershed

Note: Only data collected in a random design was used for this analysis. Benthic Index of Biotic Integrity scores are averaged over five indices of watersheds depending on data density.

Map showing Average Benthic Index of Biotic Integrity (B-IBI) scores for Chesapeake Bay sub-watersheds, categorized by color: Excellent (Green), Good (Yellow), Fair (Orange), Poor (Red), Very Poor (Dark Red), and No Score (Grey). The map includes major cities (Annapolis, Baltimore, Washington, D.C., Norfolk, Salisbury, Virginia Beach, Richmond, Martinsburg, Lexington) and the Chesapeake Bay watershed boundary. An inset map shows the location of the Chesapeake Bay watershed within the Eastern United States.

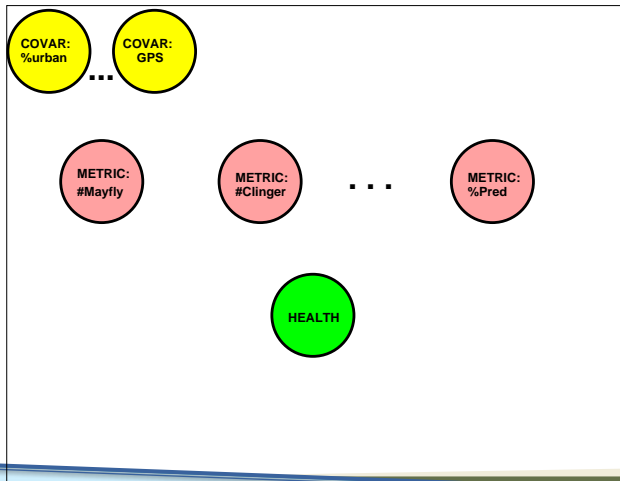
Scale: 0 to 100 Miles / 0 to 100 Kilometers

UTM Zone 18Q, NAD83

Created by J2 & P-M, 05/13/2013

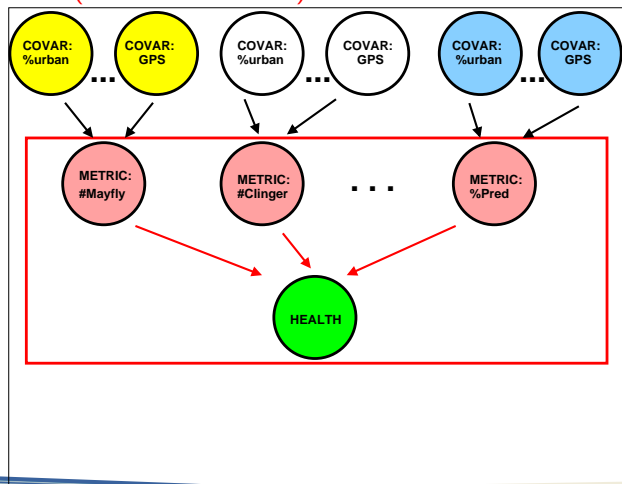
VIMS | **WILLIAM & MARY**
VIRGINIA INSTITUTE OF MARINE SCIENCE

Chessie BIBI & other conventional report-card approaches



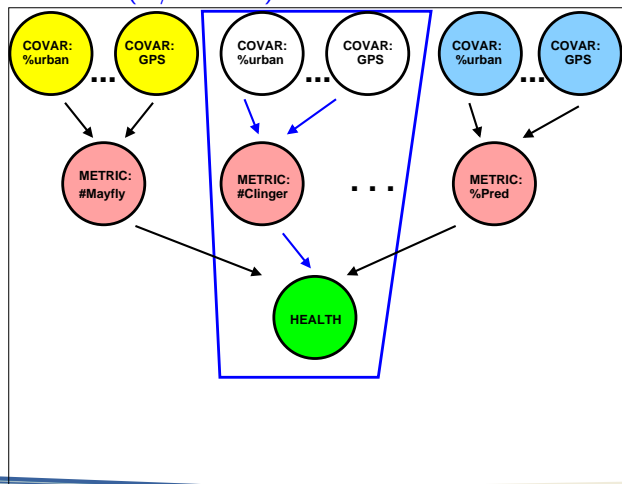
Chessie BIBI & other conventional report-card approaches

BIBI (multimetric index)



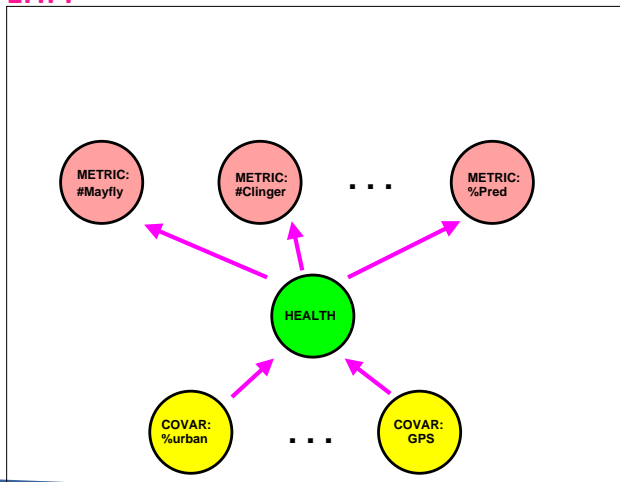
Chessie BIBI & other conventional report-card approaches

RivPACS (O/E index)



Model-based Latent Health Factor Index

LHFI



Model-based Latent Health Factor Index

LHFI modeling is a framework

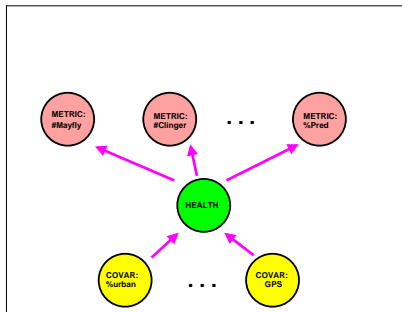
- different ecosystems may require different model structures

Model-based Latent Health Factor Index

LHFI modeling is a framework

- different ecosystems may require different model structures
 - ▶ see tinyurl.com/chiu-lhfi

Model-based Latent Health Factor Index



Environmetrics

The official journal of The International Environmetrics Society
An Association of The International Statistical Institute

Research Article

Latent health factor index: a statistical modeling approach for ecological health assessment

Grace S. Chiu^{1,*}, Peter Guttorp², Anton H. Westveld³, Shahedul A. Khan⁴, Jun Liang⁵

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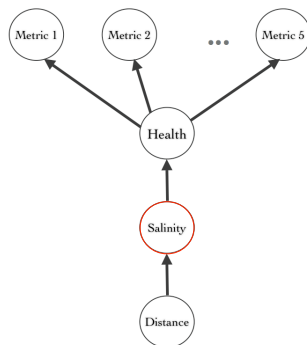
Issue



Environmetrics

Volume 22, Issue 3, pages
243–255, May 2011

Model-based Latent Health Factor Index



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PLOS ONE

Model-Based Assessment of Estuary Ecosystem Health Using the Latent Health Factor Index, with Application to the Richibucto Estuary

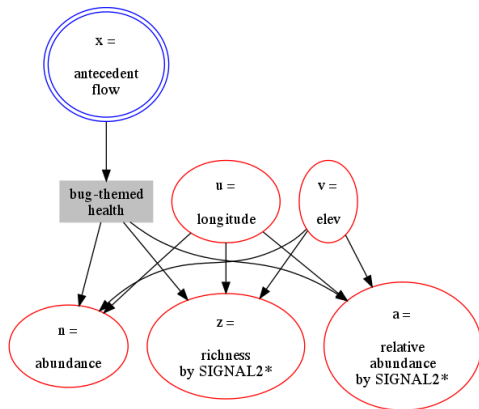
Grace S. Chiu^{1*}, Margaret A. Wu², Lin Lu³

¹ CSIRO Mathematics, Informatics and Statistics, Commonwealth Scientific and Industrial Research Organisation (CSIRO), Canberra, Australian Capital Territory, Australia, ² Business Methods Survey Division, Statistics Canada, Ottawa, Ontario, Canada, ³ McGregor GeoScience, Bedford, Nova Scotia, Canada

Abstract

The ability to quantitatively assess ecological health is of great interest to those tasked with monitoring and conserving ecosystems. For decades, biomonitoring research and policies have relied on multimetric health indices of various forms. Although indices are numbers, many are constructed based on qualitative procedures, thus limiting the quantitative rigor of the practical interpretations of such indices. The statistical modeling approach to construct the latent health factor index (LHFI) was recently developed. With ecological data that otherwise are used to construct conventional multimetric indices,

Model-based Latent Health Factor Index

R^G

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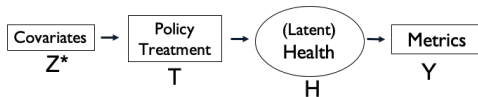
Redefining the concept of ecological health: assessment and prediction of health as model parameters at multiple spatial scales across a continental-scale river basin

September 2014

Conference: 99th Ecological Society of America Annual Meeting 2014

● Grace S. Chiu · ● Stuart E Bunn · ● Fran Sheldon

Model-based Latent Health Factor Index



arXiv.org > stat > arXiv:2009.12217

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Statistics > Methodology

[Submitted on 24 Sep 2020]

Latent Causal Socioeconomic Health Index

F. Swen Kuh, Grace S. Chiu, Anton H. Westveld

This research develops a model-based Latent Causal Socioeconomic Health (LACSH) index at the national level. We build upon the latent health factor index (LHFI) approach that has been used to assess the unobservable ecological/ecosystem health. This framework integratively models the relationship between metrics, the latent health, and the covariates that drive the notion of health. In this paper, the LHFI structure is integrated with spatial modeling and statistical causal modeling, so as to evaluate the impact of a continuous policy variable (mandatory maternity leave days and government's expenditure on healthcare, respectively) on a nation's socioeconomic health, while formally accounting for spatial dependency among the nations. A novel visualization technique for evaluating covariate balance is also introduced for

Model-based Latent Health Factor Index

A *ASSESSMENT: appropriate interpretation of a suite of biotic metrics (e.g., species richness/abundance)*

P *PREDICTION: modeling biotic-to-biotic and/or abiotic-to-biotic relations*

Model-based Latent Health Factor Index

A *ASSESSMENT: appropriate interpretation of a suite of biotic metrics (e.g., species richness/abundance)*

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Conventional approaches regard **A&P** as SEPARATE procedures

Model-based Latent Health Factor Index

A *SSESSMENT*: appropriate interpretation of a suite of biotic metrics (e.g., species richness/abundance)

P *REDICTION*: modeling biotic-to-biotic and/or abiotic-to-biotic relations

Conventional approaches regard **A&P** as SEPARATE procedures

My biomonitoring research:

To facilitate evidence-based policy-making

⇒ rigor

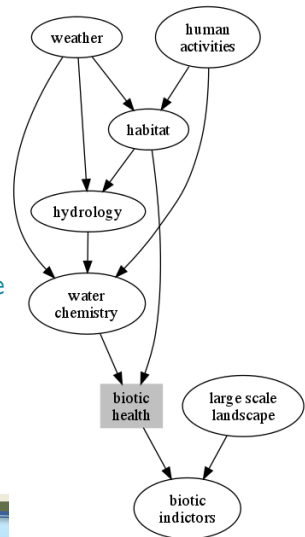
⇒ development of single hierarchical model

2. Examples of LHFI work

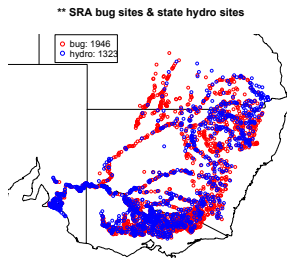
While at CSIRO: Murray-Darling Basin

I was developing model for

- Ovals are data
- HEALTH is model parameter
 - ▶ to be estimated
- Model handles spatial misalignment over multiple spatial and ecological scales
- Model-based interpolation of biotic response when samples are missing
 - ⇒ cost effective,
 - rigor in uncertainty propagation

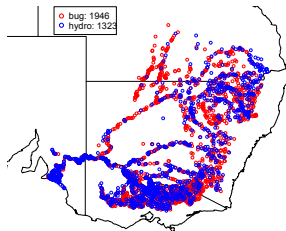


While at CSIRO: Murray-Darling Basin

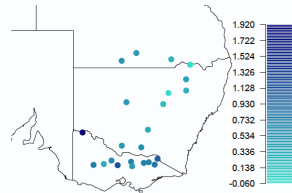
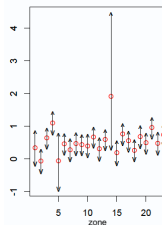


While at CSIRO: Murray-Darling Basin

** SRA bug sites & state hydro sites



LHFI 95% cred int



While at CSIRO: Murray-Darling Basin

Key model statements:

$$H_{ijt} = \phi_i + \beta_i x_{ijt} + \varepsilon_{ijt} \quad H_i := \phi_i + \beta_i \bar{x}_{i..}$$

x : antecedent log(hydro discharge) $\{\phi_i\} \sim \text{mean-0 CAR}$

$$\beta_i \sim N(\beta, \omega_b^2) \quad \varepsilon_{ijt} \sim N(0, \gamma_i \sigma_e^2)$$

$$y_{rijtk} = \alpha_{0r} + \alpha_{1r} u_{ij} + \alpha_{2r} v_{ij} + \alpha_{3r} H_{ijt} + \eta_{rijtk}$$

$$\begin{bmatrix} \eta_{1ijtk} \\ \eta_{2ijtk} \\ \eta_{3ijtk} \end{bmatrix} \sim \text{MVN}(\mathbf{0}, \mathbf{\Sigma}_i)$$

$r \in \{1=\text{log-abund.}, 2=\text{weighted rich.}, 3=\text{weighted rel. abund.}\}$

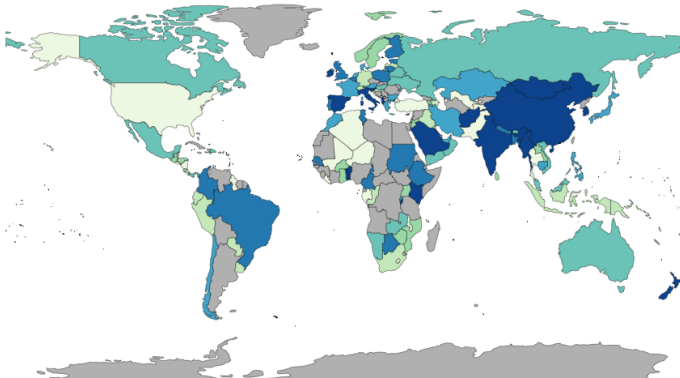
u, v : longitude, log(elevation)

While at ANU/VIMS: LACSH

Latent **C**ausal **S**ocio-economic **H**health

While at ANU/VIMS: LACSH

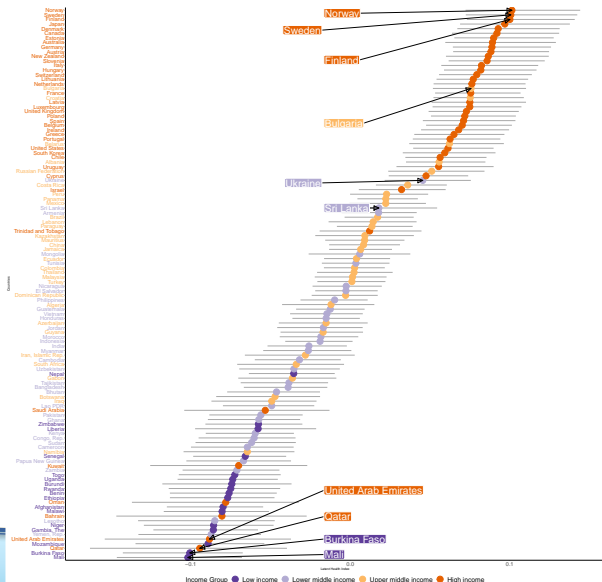
Latent Causal Socio-economic Health



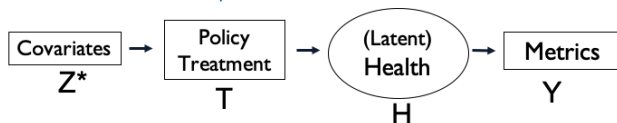
While at ANU/VIMS: LACSH

Causal variable:

Mandatory
maternity leave days



While at ANU/VIMS: LACSH



$$y_i | a, H_i, \Sigma_Y \stackrel{ind.}{\sim} \text{MVN}(aH_i, \Sigma_Y)$$

$$H | \beta, T, R, \Sigma_H \sim \text{TMVN}(\mu, \Sigma_H) \mathbb{1}\{H_{anc} < 0\}$$

$$T_i | Z_i^*, \gamma, \sigma_T^2 \sim N(Z_i^* \gamma, \sigma_T^2)$$

$$\text{where } [\mu]_i = \beta_0 + \beta_1 T_i + \beta_2 T_i^2 + \beta_3 R_i + \beta_4 R_i^2 + \beta_5 T_i R_i$$

$$R_i = r(T_i, \gamma, Z_i^*, \sigma_T^2) = \frac{1}{\sqrt{2\pi\sigma_T^2}} \exp\left(-\frac{1}{2\sigma_T^2}(T_i - Z_i^* \gamma)^2\right)$$

$$\Sigma_H = \sigma_H^2 \Omega(d, \phi)$$

$$\Omega(d, \phi) = \begin{bmatrix} 1 & \rho_{12} & \cdots & \rho_{1n} \\ \rho_{21} & 1 & \ddots & \vdots \\ \vdots & \ddots & \ddots & \rho_{n-1,n} \\ \rho_{n1} & \cdots & \rho_{n,n-1} & 1 \end{bmatrix}$$

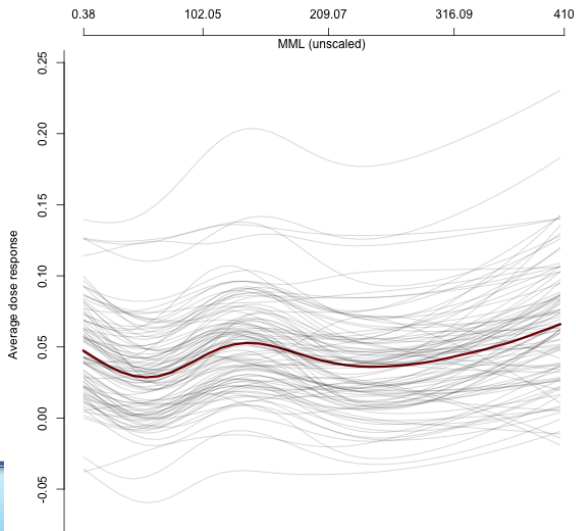
$$\rho_{nm} = \exp(-d_{nm}/\phi) = \rho_{mn}$$

← causal framework:
generalized propensity score

While at ANU/VIMS: LACSH

Causal relationship:

Health vs. Maternity Leave Days



LHFI/LACSH in a nutshell

LHFI/LACSH in a nutshell

- Single hierarchical model / one-stop shop
 - ▶ unifies various aspects of health
 - ▶ rigor in uncertainty propagation
- Health is model parameter
 - ▶ formal uncertainty quantification
- No big deal when biotic data are missing
- Rigorous assessment of policy (causal) effects on health

References

- tinyurl.com/chiu-lhfi
- Search for [Grace S Chiu](#) on Research Gate or Google Scholar