

# *Optimization Update: **Transfer Learning***

Kalyanmoy Deb, Pouyan  
Nejadhashemi, Gregorio  
Toscano, and Hoda Razavi



# *Agenda*

- Our current status
- "Innovization" concept for knowledge discovery
- Re-optimization using learned knowledge
- Transfer Learning to solve similar other problems quickly
- Results on above concepts on some counties
- Conclusions

# Timeline of the Project

[illegible]

We are here

## **Task 3: Multi-state implementation using machine learning and parallel computing platforms**

3.1 Comparative study to choose a few best performing methods

3.2 Scalability to state and watershed level scenarios

**3.3 “Innovization” approach for improving scalability**

3.4 Distributed computing approach for improving scalability

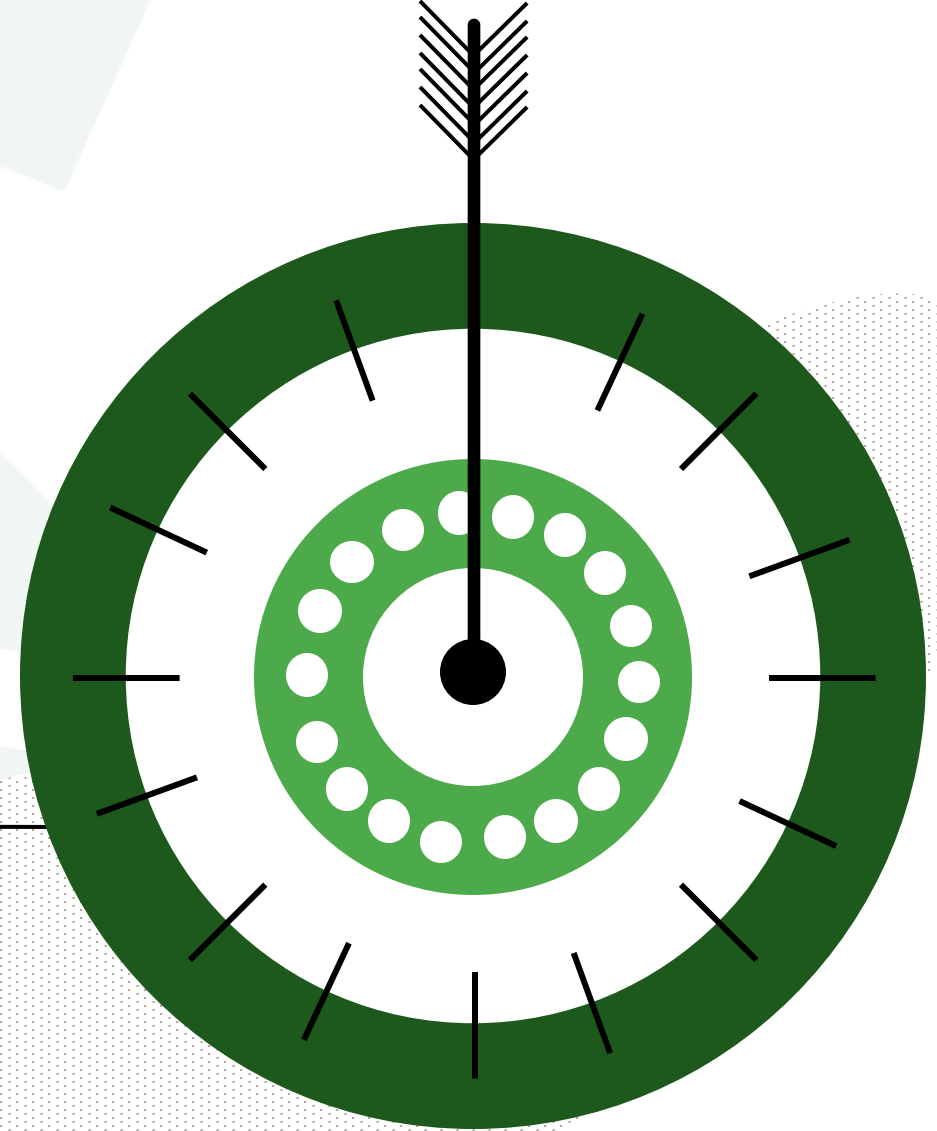
# ***Timeline of the Project***



# Research Goal



To **reduce search space for optimization** by creating new knowledge based on physical characteristics of a study area.

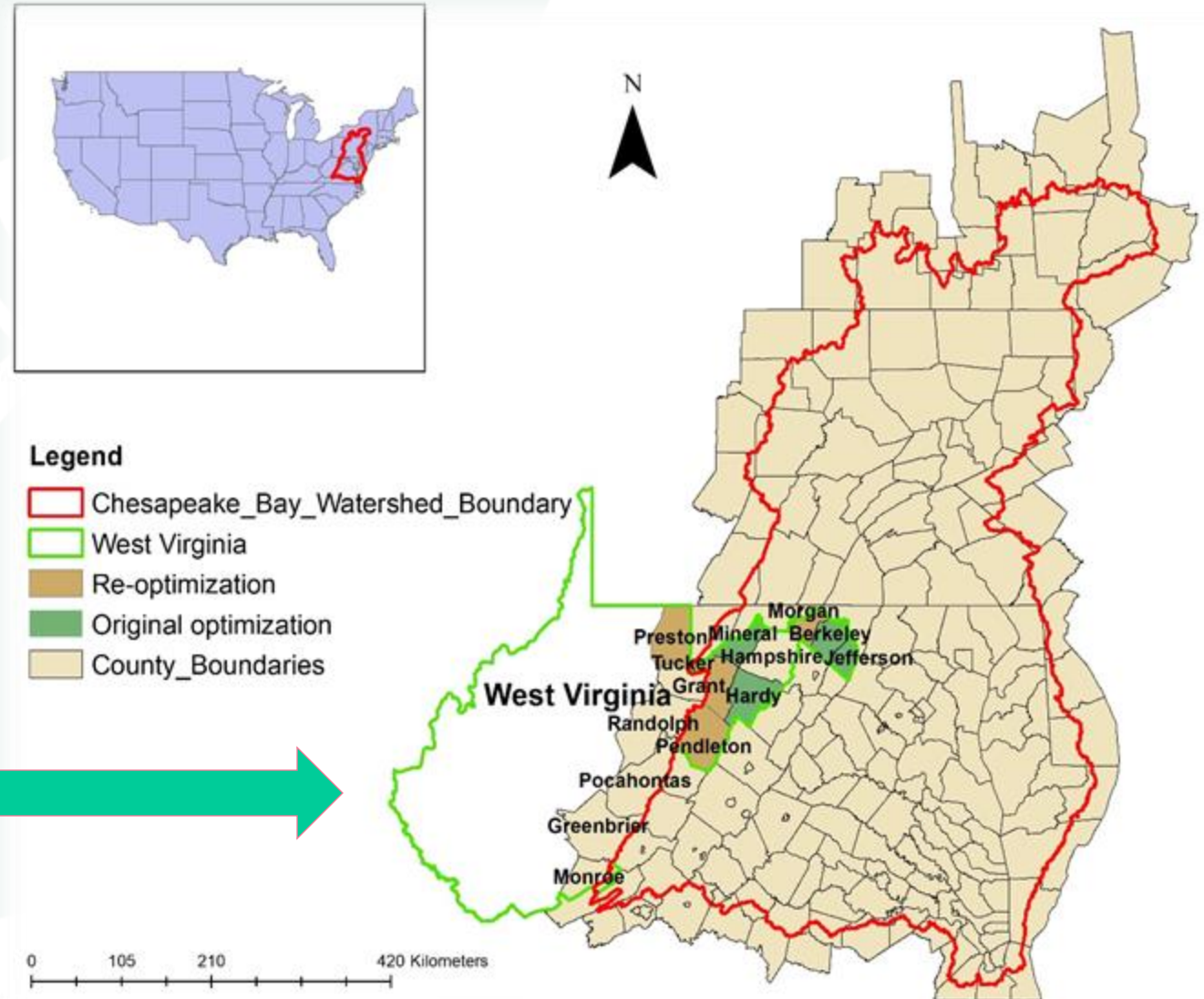




# Methodology

# Chesapeake Bay Watershed

- The **largest estuary** in the United States and the **third-largest** in the world.
- Over **300 counties**
- **WEST VIRGINIA**



# Problem Significance (Search Space Complexity)

- Let's talk about **one county out of 300**



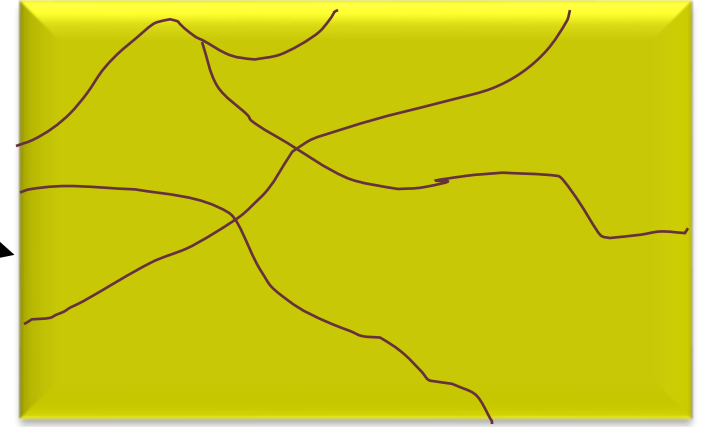
County





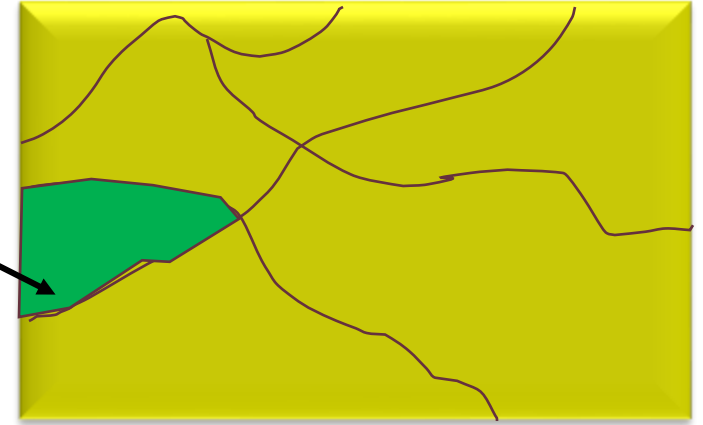
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- Each landriver segment can **accept up to 200 BMPs options**

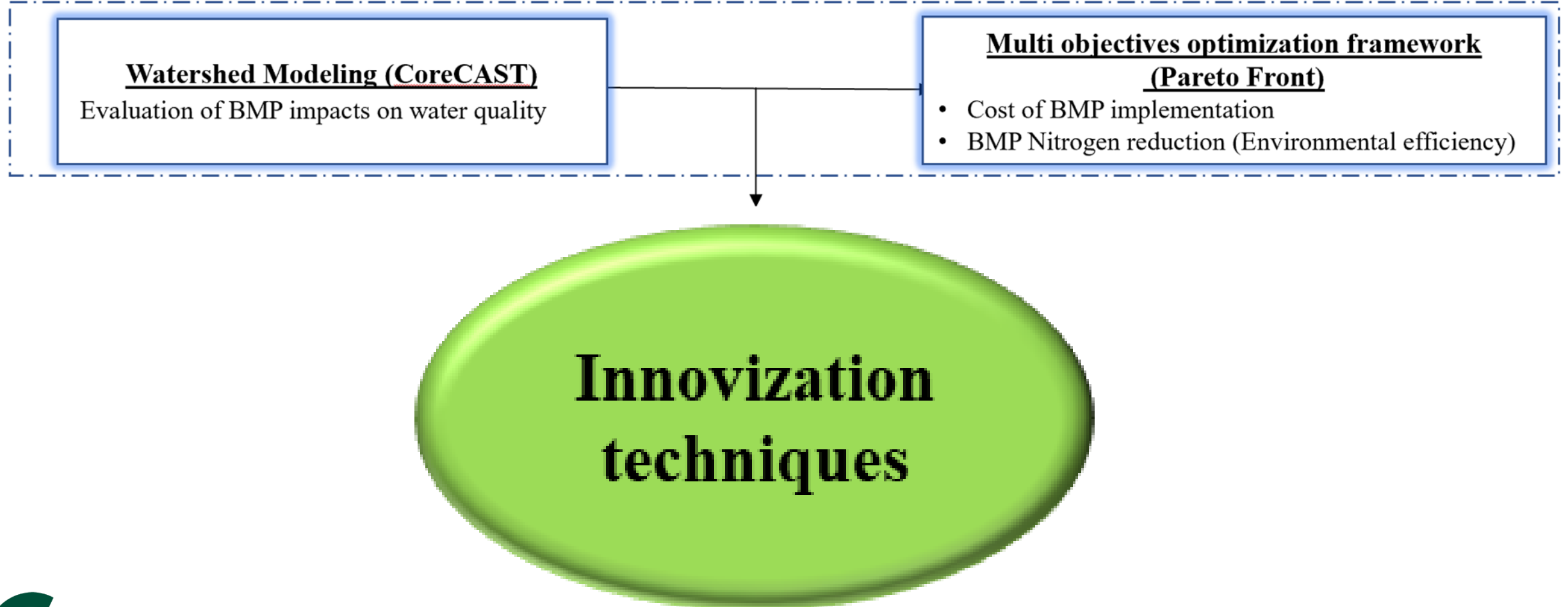


# Problem Significance (Search Space Complexity)

- Each county on average has 10 land-river segments,
- Each landriver segment can accept up to 200 BMPs options (i, e, variables)
- Each landriver segment **has 50 land use options**
- Making the overall search space for a county to have about  **$50^{2,000}$  different management options.**
- **Highly constrained:** ~more than 100,000 constraints.



# Overview of the Methodology



# Innovation through Optimization



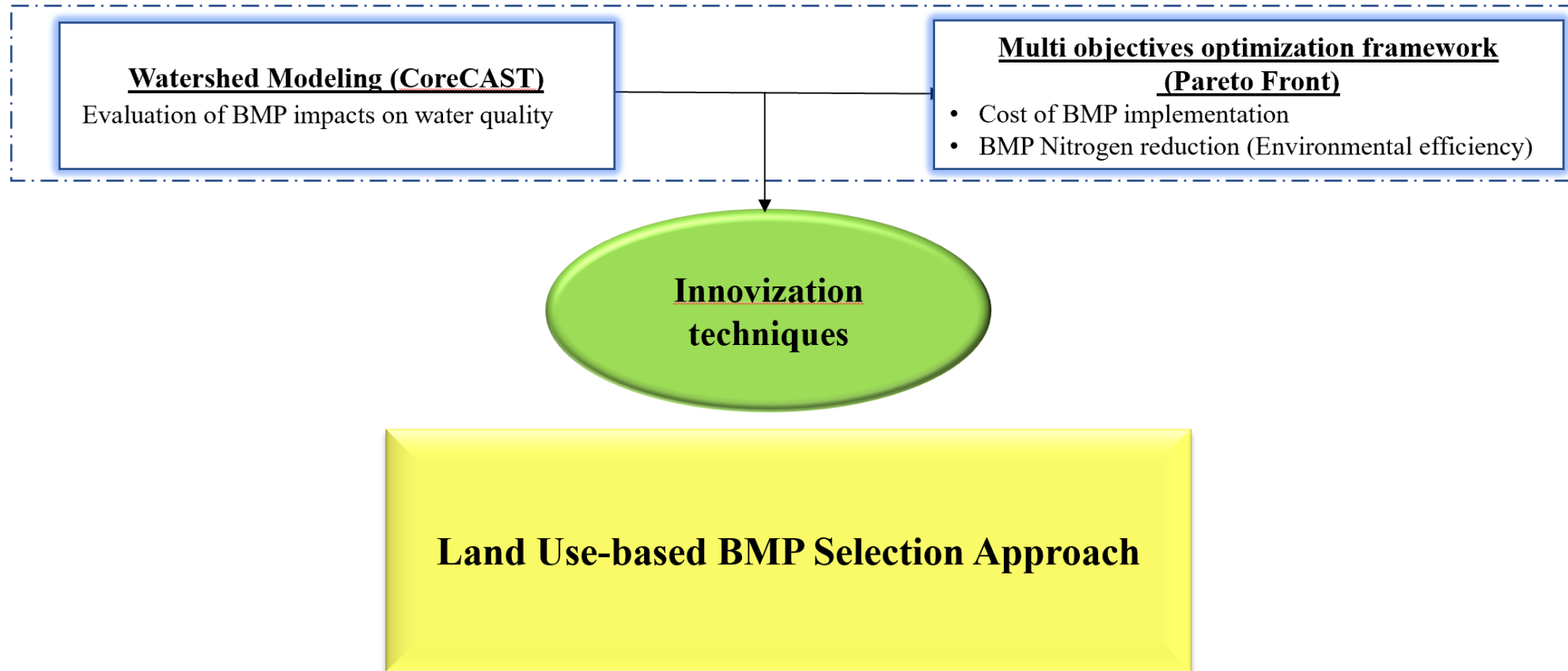
- What is innovization?

Create **new knowledge** from optimization solutions

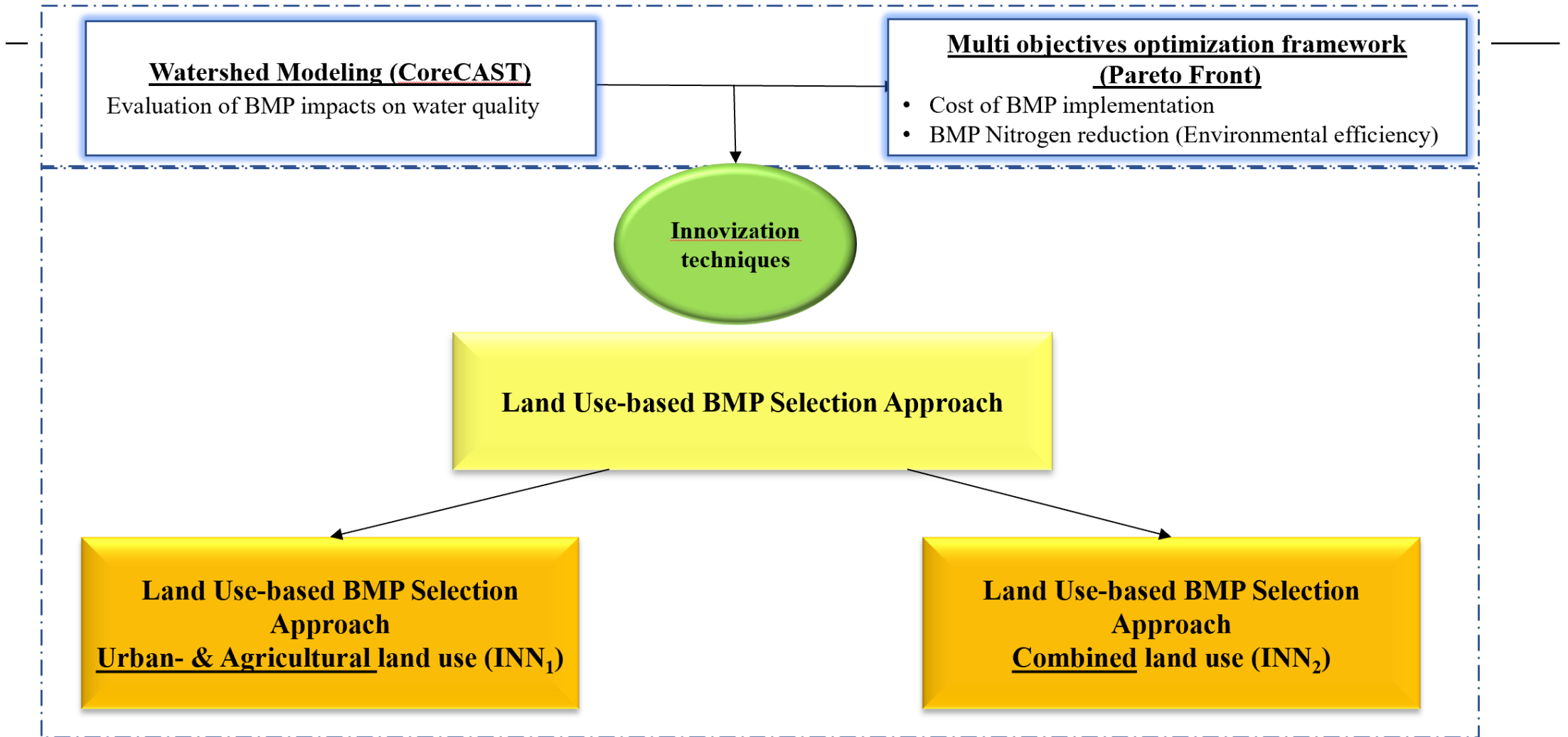




# Overview of the Methodology



# Overview of the Methodology



# Methodology

## The Land Use-based BMP Selection Approach (Innovization based on the Urban- and Agricultural-dominated Land Use Characteristics) (INN1)

We hypothesize that since urban and agricultural-dominated areas are basically **different** in terms of pollution generation, fate, and transport. Therefore, different types of BMPs should be selected to address these challenges.



# Methodology



BMP Selection ranking strategy based on Land use:



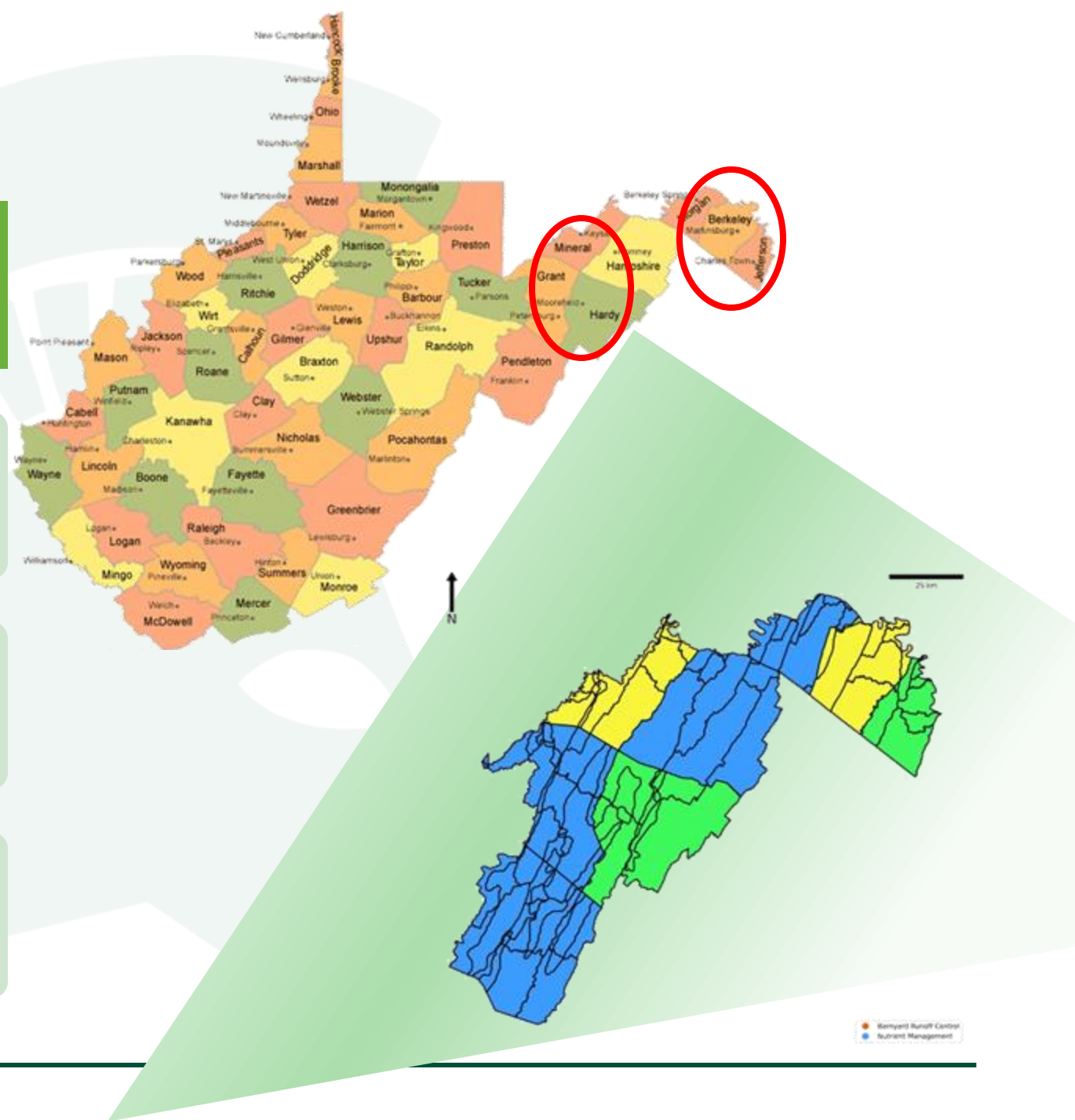
In **West Virginia**, we identified the top two counties with the highest areas of urban and agricultural land uses.



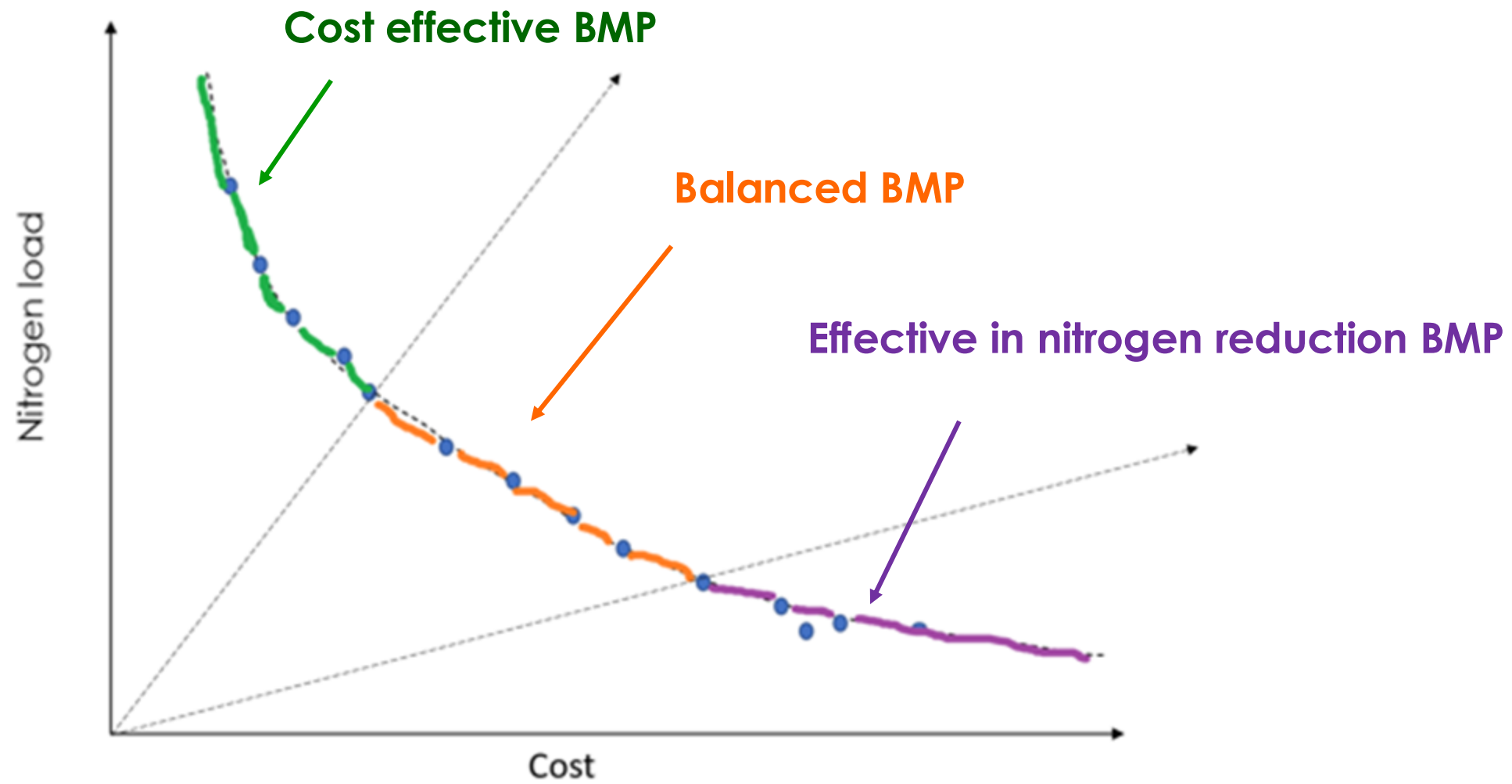
(**Berkeley and Mineral**): Urban dominated



(**Jefferson and Hardy**): Agricultural dominated



# Pareto Front



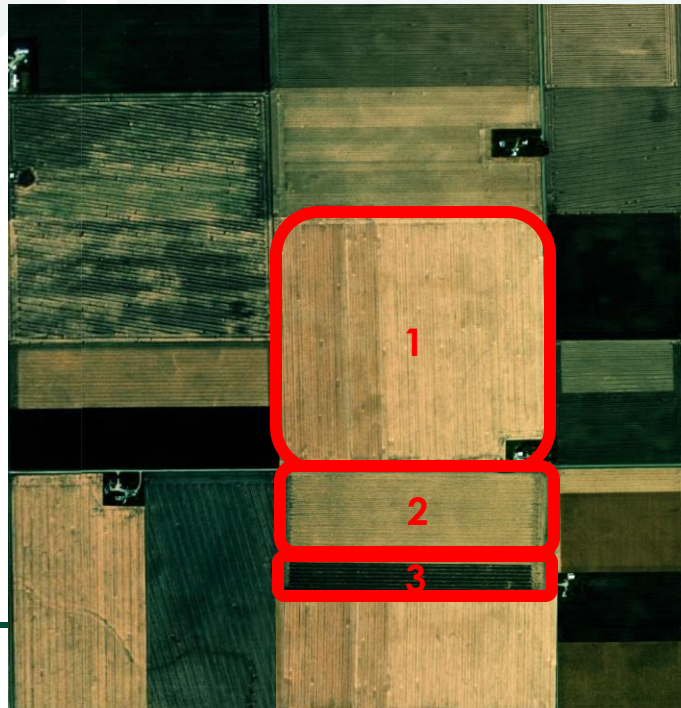


# Methodology

1

Examine different ranking methodologies to **identify the top BMPs**

- **Ranking strategy 1)** rank the top BMPs based on the **implementation acreages**;
- **Ranking strategy 2)** rank the top BMPs based on the percentage of **maximum allowable** acreages;
- **Ranking strategy 3)** rank the top BMPs based on the amount of **nitrogen reduction per dollar spent**.



# Methodology

1

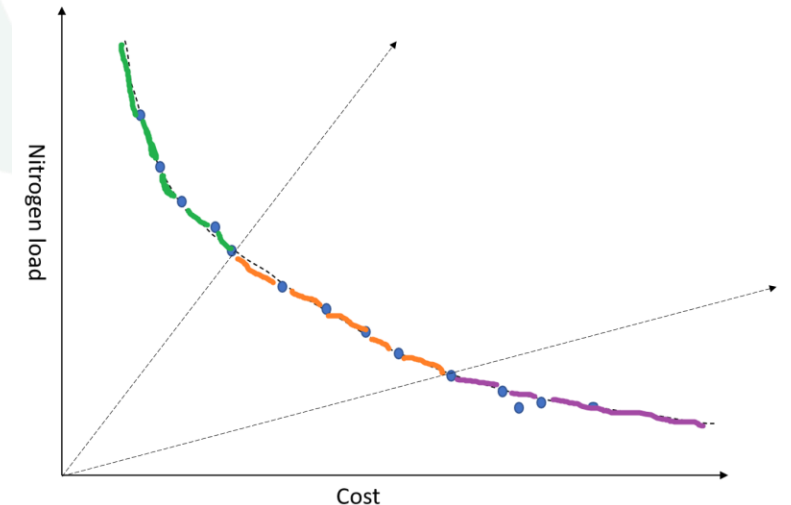
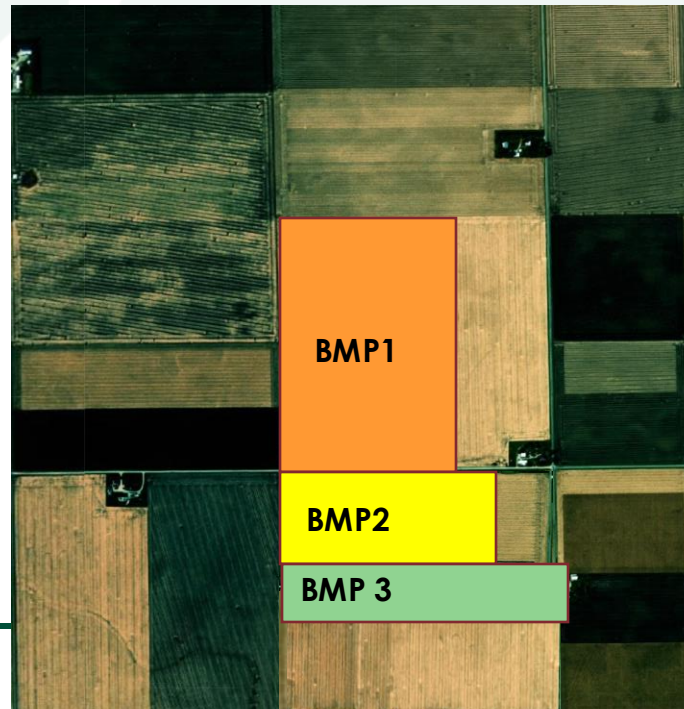
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- Ranking strategy):**

**BMP1**

**BMP2**

**BMP3**



MICHIGAN STATE  
UNIVERSITY

# Methodology

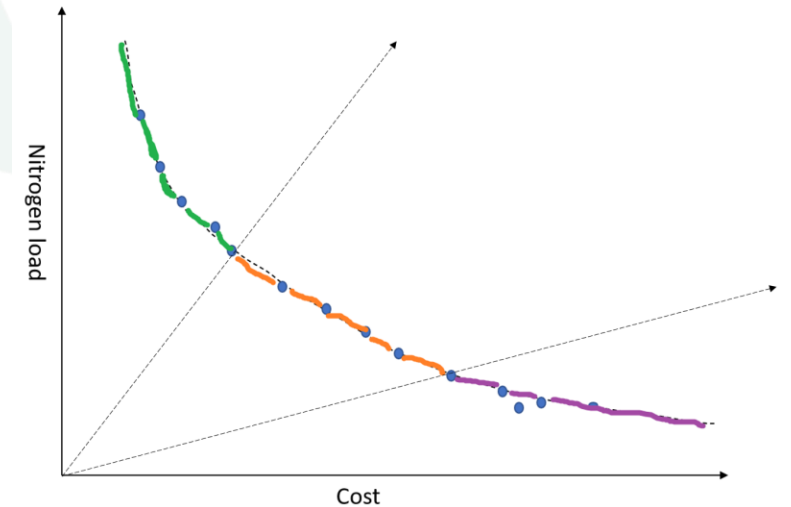
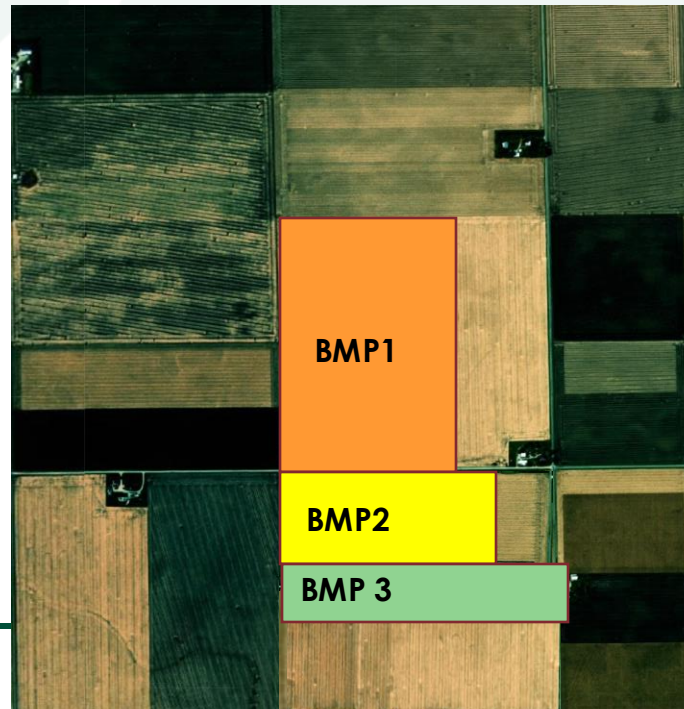
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Ranking strategy 2):

**BMP3**  
**BMP2**  
**BMP1**



# Methodology

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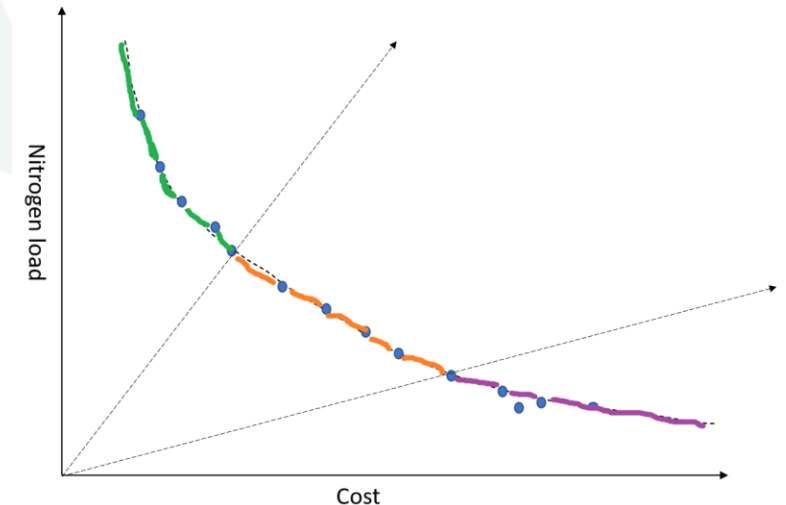
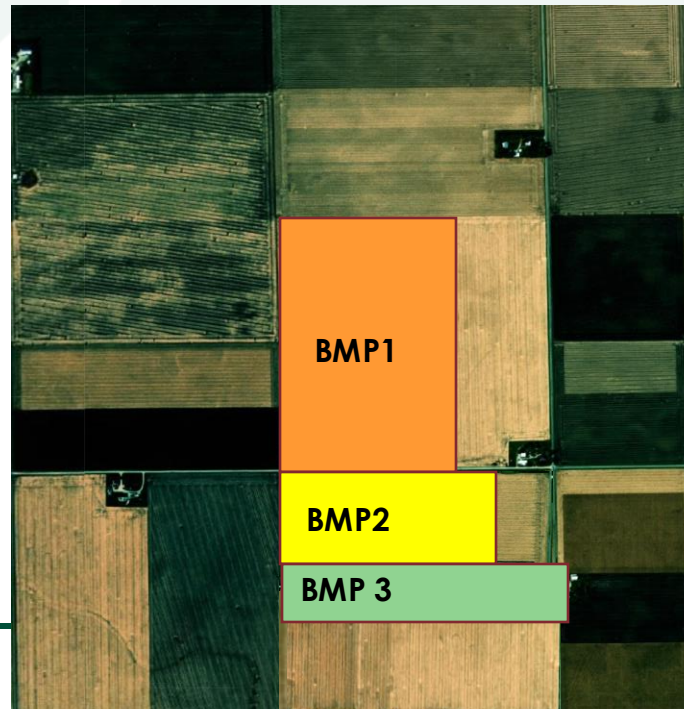
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**Ranking methodology3):**

**BMP2 (\$12/lb N)**

**BMP3 (\$15/lb N)**

**BMP1 (\$24/lb N)**



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# Methodology

## Land Use-based BMP Selection Approach (Innovization based on the Combined Urban- and Agricultural-dominated Land Use Characteristics) (INN2)

### Development of Strategies:

1. **INN2-STG1**: Combines BMPs with the **highest implementation acreages** from **both** land use types.
2. **INN2-STG2 & INN2-STG3**: Use information from strategies focusing on **maximum area of implementation** and **cost-effectiveness in nitrogen reduction**, respectively.
3. **INN2-STG4**: A hybrid strategy that combines BMPs from INN1-STG1 & INN1-STG3, considering both **high implementation acreages and cost-effectiveness**.





# Methodology

## Statistical methods

- ❑ The **base/control scenario** considering **all potential BMPs (up to 200)** and the **innovization method (INN1 & INN2)** consider up to **10 BMPs**.
- ❑ Compare the new INN1 and INN2 approaches with the **regular optimization (Control)**

## The Wilcoxon-Mann-Whitney test method



# Results (INN1) Urban vs. Ag

# Results

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Examine different ranking methodologies to **identify the top BMPs**,

**Table: Top choice BMPs based on the all three-ranking methodology**

| Urban Top-Ranked Counties                         |   |  | Agricultural Top-Ranked Counties         |   |  |
|---|---|--|--|---|--|
| Strategy 1  | Strategy 2                                | Strategy 3                               | Strategy 1                               | Strategy 2                              | Strategy 3                               |
| Nutrient Management Plan High-Risk Lawn           | Barnyard Runoff Control                   | Nutrient Management Plan High-Risk Lawn  | Nutrient Management Plan High-Risk Lawn  | Barnyard Runoff Control                 | Nutrient Management Plan High-Risk Lawn  |
| Off-Stream Watering Without Fencing               | Agricultural Stormwater Management        | Off-Stream Watering Without Fencing      | Off-Stream Watering Without Fencing      | Nutrient Management Plan High-Risk Lawn | Off-Stream Watering Without Fencing      |
| Nutrient Management N Timing                      | Nutrient Management Plan High-Risk Lawn   | Nutrient Management N Rate               | Nutrient Management N Timing             | Nutrient Management N Rate              | Nutrient Management N Rate               |
| Precision Intensive Rotational/Prescribed Grazing | Soil Conservation and Water Quality Plans | Forest Harvesting Practices              | Nutrient Management N Rate               | Nutrient Management N Timing            | Nutrient Management N Timing             |
| Cover Crop Traditional Rye Early Drilled          | Off-Stream Watering Without Fencing       | Nutrient Management N Timing             | Cover Crop Traditional Rye Early Drilled | Agricultural Stormwater Management      | Cover Crop Traditional Rye Early Drilled |
| Nutrient Management N Rate                        | Nutrient Management N Placement           | Cover Crop Traditional Rye Early Drilled | Nutrient Management N Placement          | Nutrient Management N Placement         | Nutrient Management N Placement          |
| Nutrient Management N Placement                   | Nutrient Management N Rate                | Nutrient Management N Placement          | Barnyard Runoff Control                  | Off-Stream Watering Without Fencing     | Cover Crop Traditional Rye Early Other   |



**All three-ranking methodologies:**



# Results

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# Results:

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Table: Top choice BMPs based on the all **three-ranking methodology**



All three-ranking methodologies:



More than once  
BMPs



Once repeated  
BMPs

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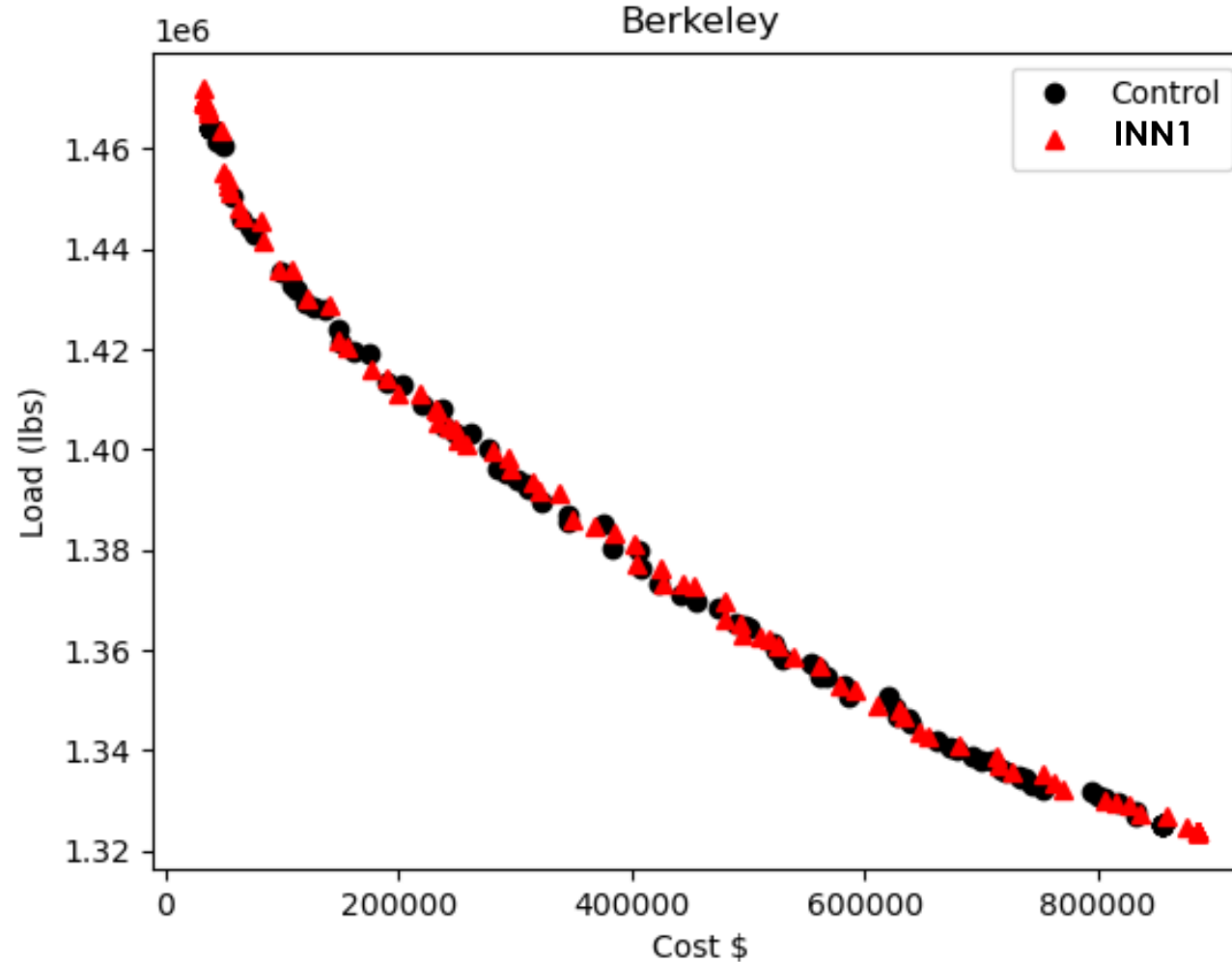
# Results:

Reduce the optimization variables & search space

|           | Control | INN1     |
|-----------|---------|----------|
| Berkeley  | 14,090  | 510 (3%) |
| Hardy     | 18,607  | 725 (3%) |
| Jefferson | 12,303  | 456 (3%) |
| Mineral   | 20,260  | 765 (3%) |



# Compare control against INN 1 (Berkeley County)



# Statistical analysis

Compare the new INN1 approach with the regular optimization (Control/Base)

The Wilcoxon-Mann-Whitney test method (p-value)

| Innovization | Urban Dominated counties |          | Agricultural Dominated counties |          | All counties |
|--------------|--------------------------|----------|---------------------------------|----------|--------------|
|              | Berkeley                 | Mineral  | Jefferson                       | Hardy    |              |
| INN1         | 0.065                    | 4.08E-05 | 0.00354                         | 4.08E-05 | 0.338        |



# Results (INN2) Combined

# Results:

## Statistical methods:

The Wilcoxon-Mann-Whitney test- Statistical analysis for INN2 section:

- P value of (Hyper volume-HV) for all four strategies for 5 and 10 top BMP (INN2) compared to the Control case

|                   | <i>Control</i>  | <i>Control</i> | <i>Control</i>   | <i>Control</i> | <i>Control</i>      |
|-------------------|-----------------|----------------|------------------|----------------|---------------------|
| <b>Strategies</b> | <b>Berkeley</b> | <b>Hardy</b>   | <b>Jefferson</b> | <b>Mineral</b> | <b>all counties</b> |
| Strategy-1-10     | 0.032986        | 0.146712       | 0.000319         | 0.050334       | 0.2654347           |
| Strategy-1-5      | 0.178967        | 0.000041       | 0.007558         | 0.000041       | 0.0060929           |
| Strategy-2-10     | 0.000041        | 0.001564       | 0.000041         | 0.083953       | 0.3380517           |
| Strategy-2-5      | 0.000041        | 0.000053       | 0.000041         | 0.000041       | 0.0060929           |
| Strategy-3-10     | 0.000041        | 0.000091       | 0.000041         | 0.000811       | 0.0060929           |
| Strategy-3-5      | 0.000646        | 0.000646       | 0.000041         | 0.000041       | 0.0060929           |
| Strategy-4-10     | 0.000319        | 0.000053       | 0.000041         | 0.118609       | 0.0060929           |
| Strategy-4-5      | 0.000041        | 0.000646       | 0.000117         | 0.000041       | 0.0060929           |



# Conclusion



# Conclusion Innovization



## 1. First Innovization Technique:

This method greatly **simplified** the **BMP selection process** by **reducing the number** from approximately 200 to just seven. This simplification aids in:

1. **Simplicity and Manageability**
2. **Reduce Optimization Constrained**

## 2. Second Innovization Technique:

This approach was **validated** across various regions, showing improved performance in adapting the innovization method beyond the initial study area.



# ***Re-Optimization with Reduced BMPs***

- **Purpose:**

- Verify that a reduced set of BMPs can still produce optimal results.
- Ensure that the simplified BMPs are still effective and efficient.

- **Validation:**

- Confirm that the selected BMPs from innovation are capable of achieving desired outcomes.
- Re-optimization ensures robustness and reliability of the reduced BMP set.

- **Efficiency Gains:**

- Faster run times due to fewer variables.
- Reduced computational effort.

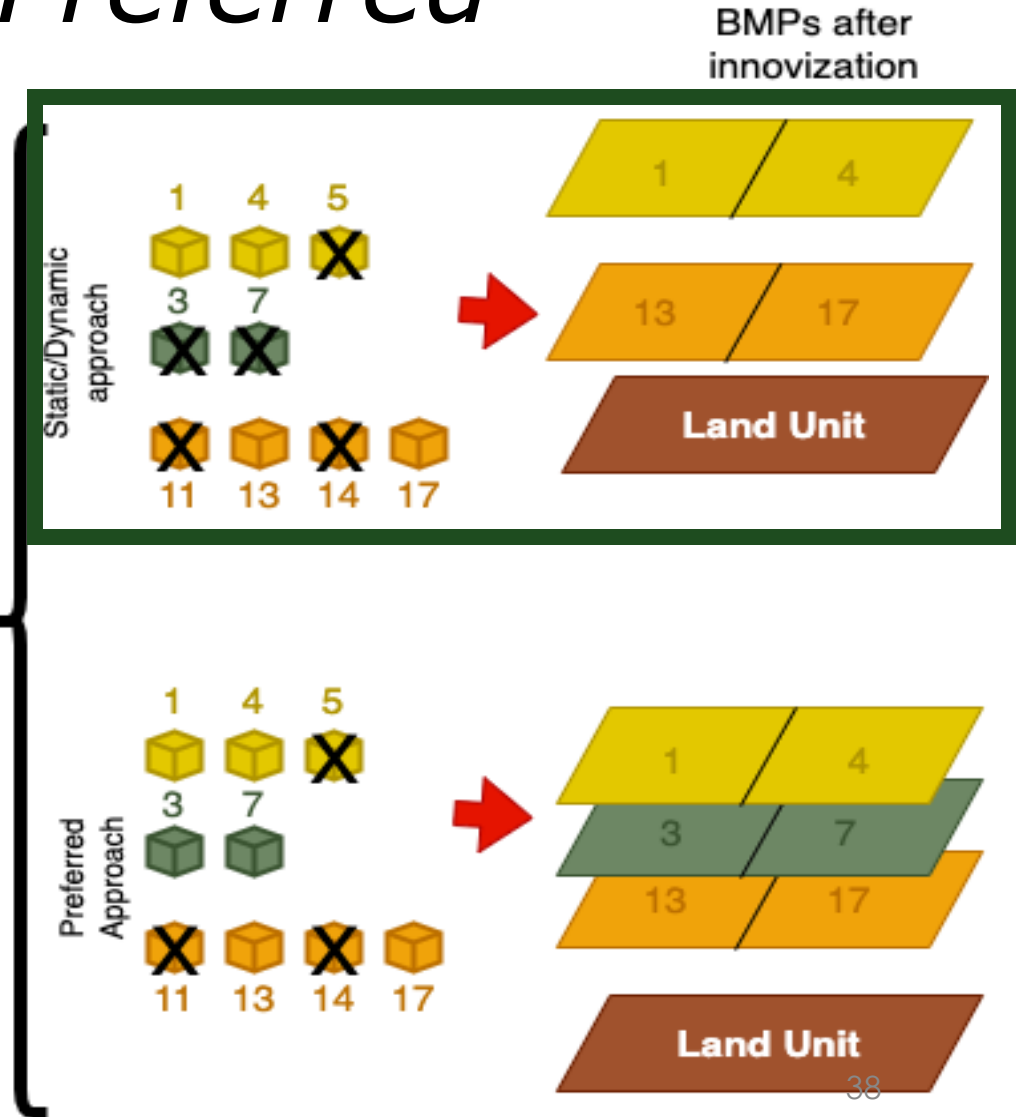
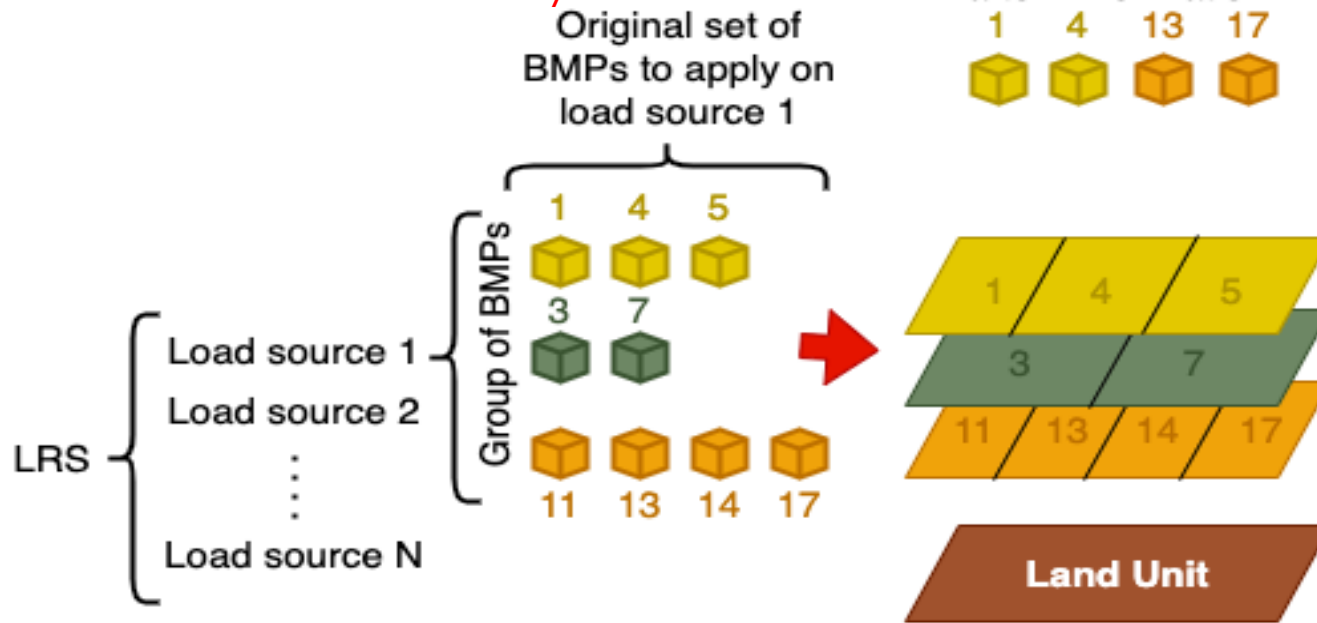
- **Quality Results:**

- Maintain or improve solution quality with fewer BMPs.
- Demonstrate that the reduced set is effective in achieving goals.

# Re-optimization Strategies

## Control/Static/Dynamic/Preferred

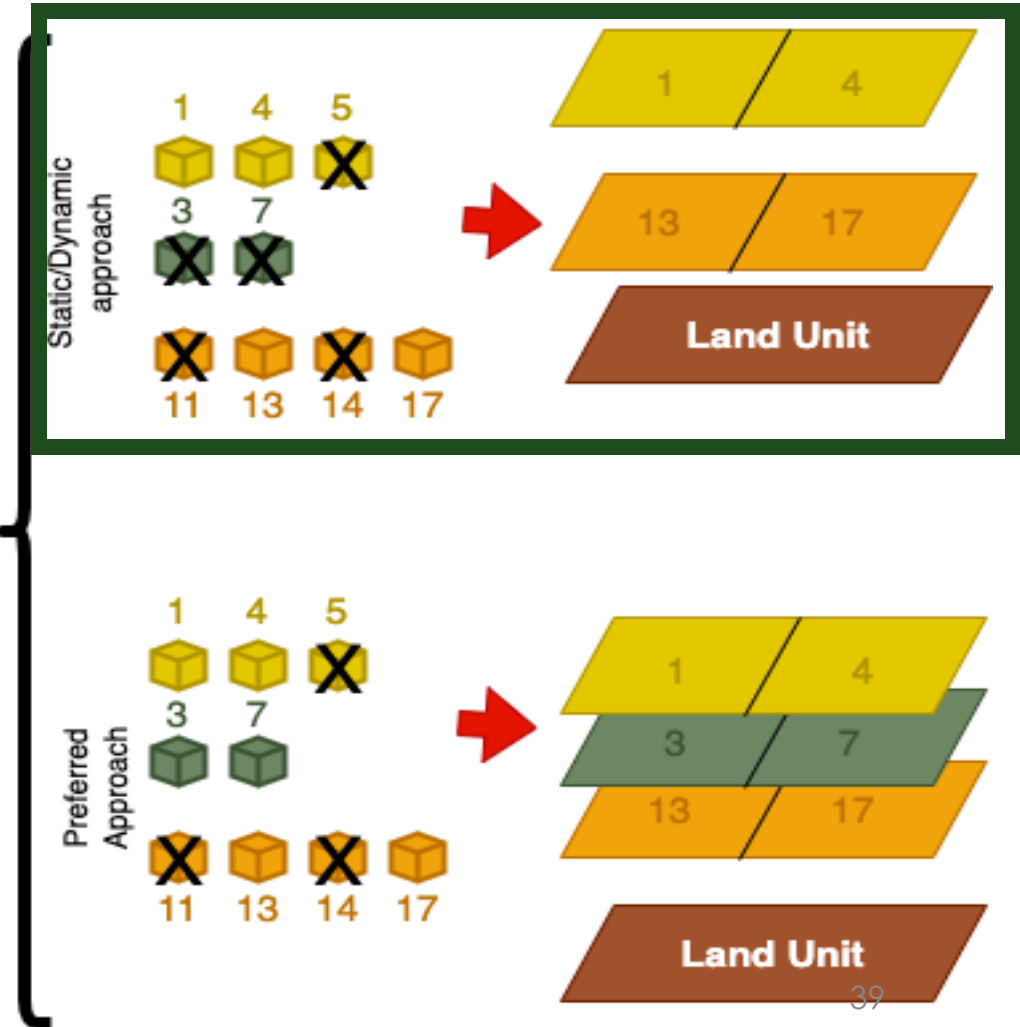
Only seven BMPs that provide the best benefit according to the innovization analysis.



# Re-optimization Strategies

## Control/Static/Dynamic/Preferred

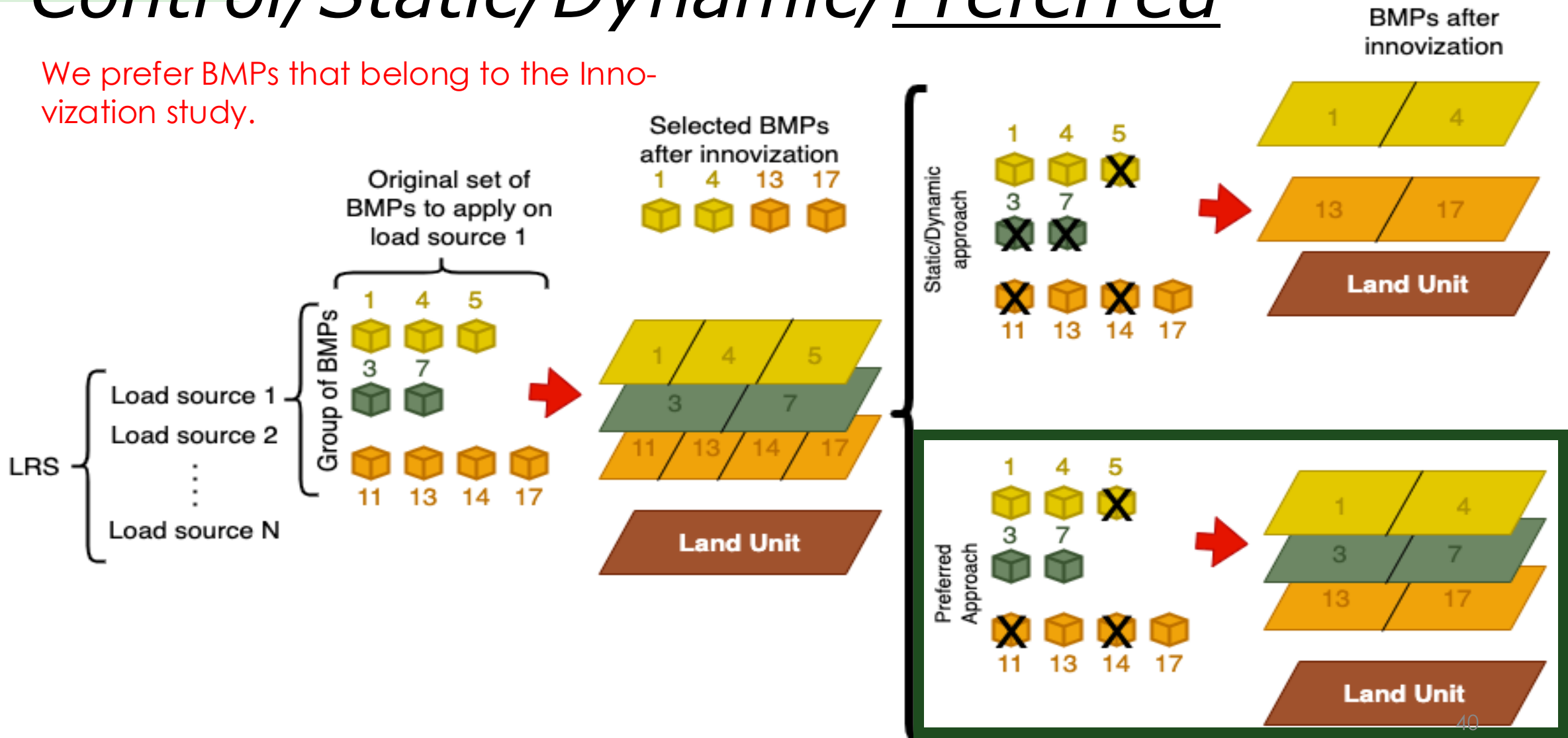
A priority list of BMPs until an accumulative percentage of 99.9% of the total implementation area is covered.



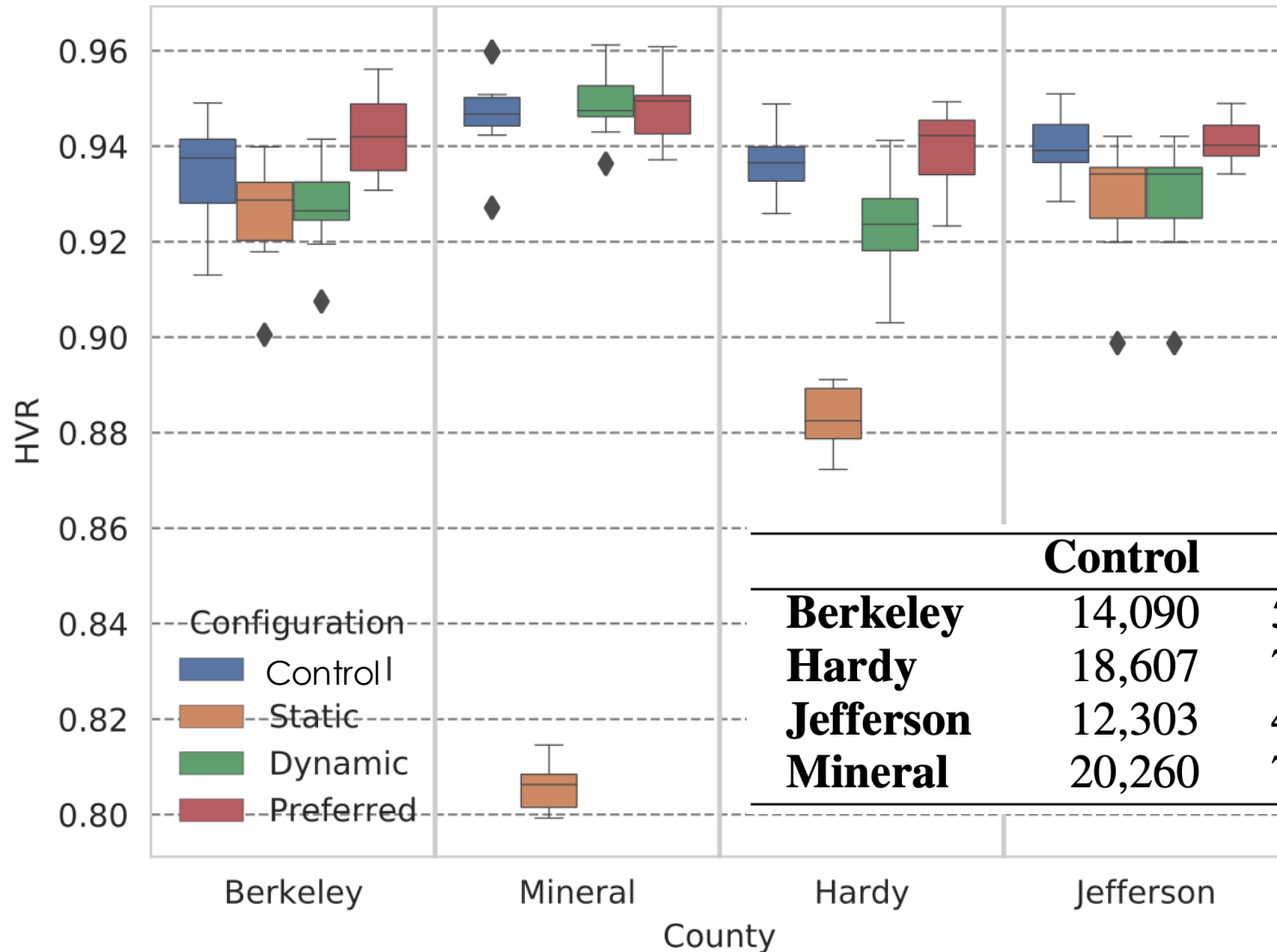
# Re-optimization Strategies

## Control/Static/Dynamic/Preferred

We prefer BMPs that belong to the Innovation study.



# Validation with Hypervolume Ratio



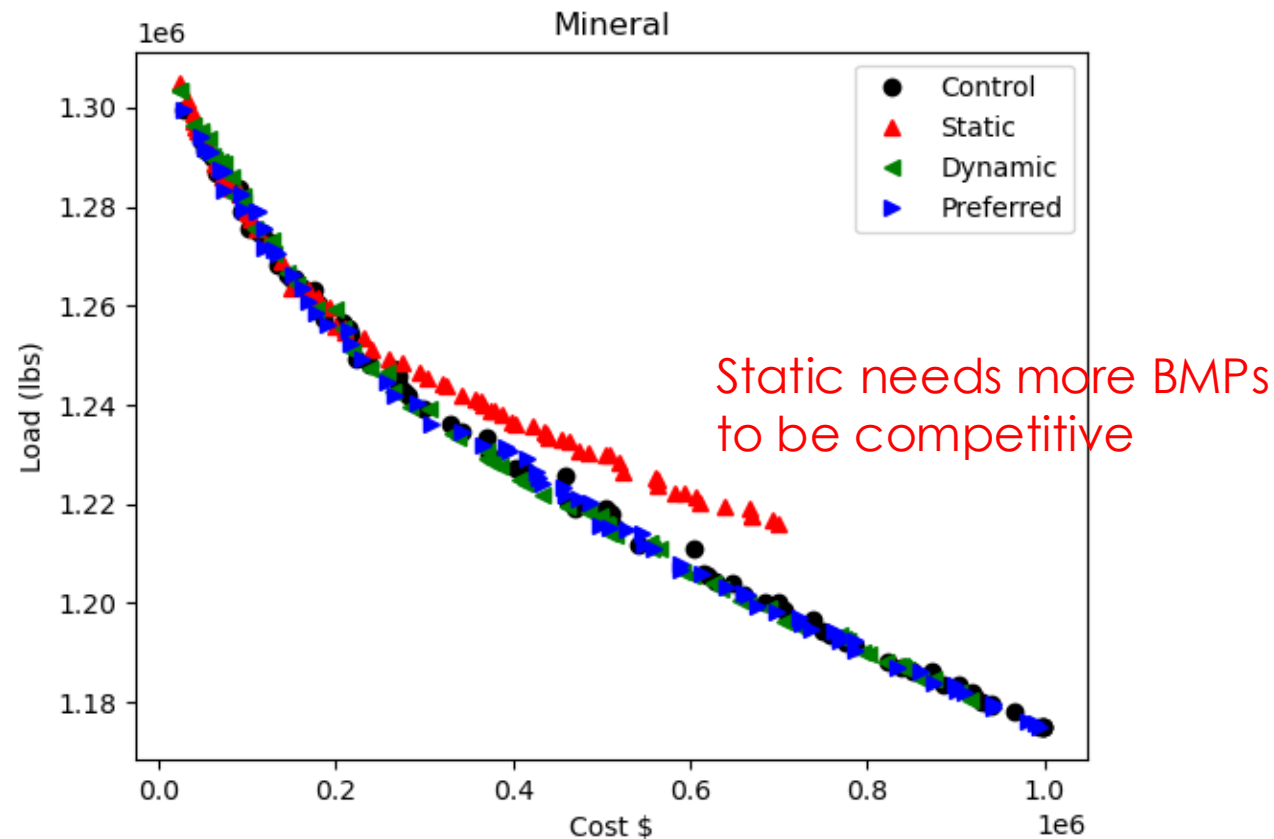
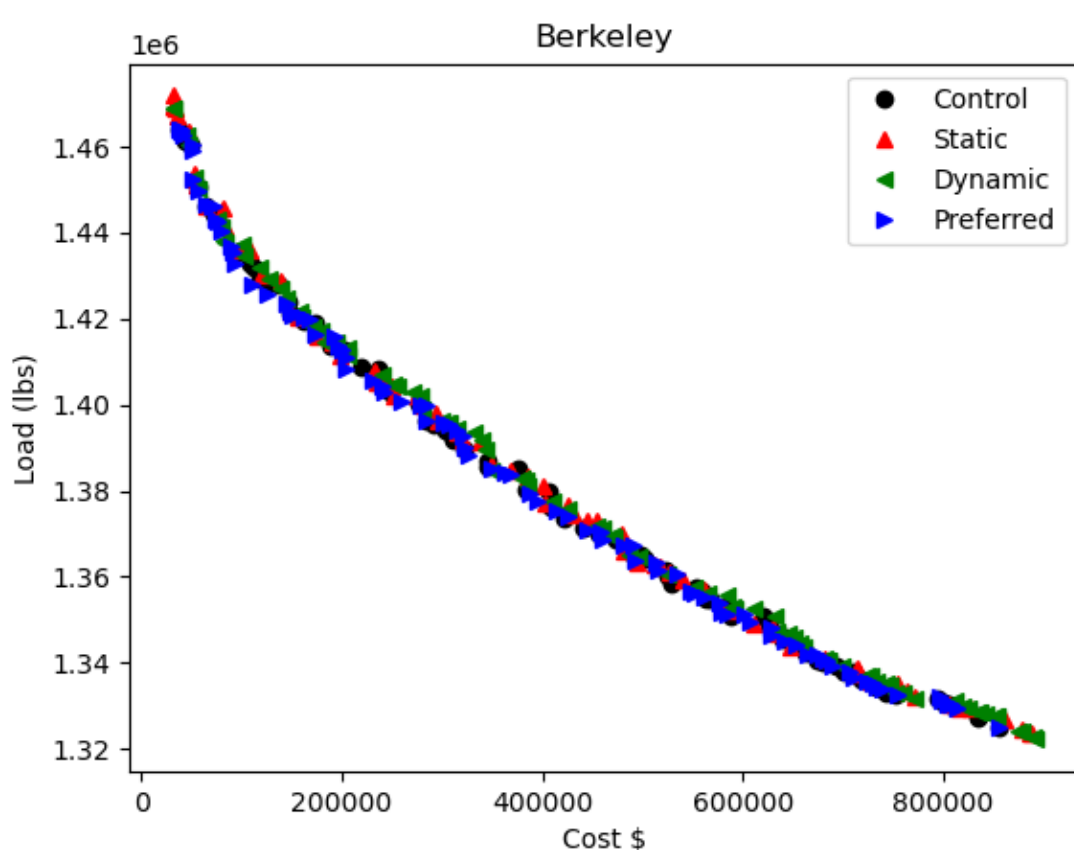
- Competitive Results
- Fraction of the variables.
- Static failed in some counties (it couldn't find a competitive solution with such a small BMP list).
- Preferred outperformed the other approaches (better exploitation of the area).

An order of magnitude less regarding the number of variables

|                  | Control | Static   | Dynamic    | Preferred   |
|------------------|---------|----------|------------|-------------|
| <b>Berkeley</b>  | 14,090  | 510 (3%) | 1,023 (7%) | 4,823 (34%) |
| <b>Hardy</b>     | 18,607  | 725 (3%) | 751 (4%)   | 5,307 (28%) |
| <b>Jefferson</b> | 12,303  | 456 (3%) | 456 (3%)   | 4,079 (33%) |
| <b>Mineral</b>   | 20,260  | 765 (3%) | 1,650 (8%) | 6,415 (31%) |



# *Pareto Fronts (Representative)*



Re-optimizing with fewer variables can produce similar performance on the large-scale problem: Our Suggestion: Preferred strategy

# ***Achievements with Re-optimization***

- With a fraction of variables, we achieve similar results
- Validated on single and multiple counties

# *Transfer Learning*

- **Definition:**

- Transfer learning is the application of knowledge gained from solving one problem to a different but related problem.

- **Simplified Explanation:**

- Imagine learning to drive a car. Once you know how to drive one car, you can easily drive any other car without having to learn from scratch again.



# ***Why Use Transfer Learning?***

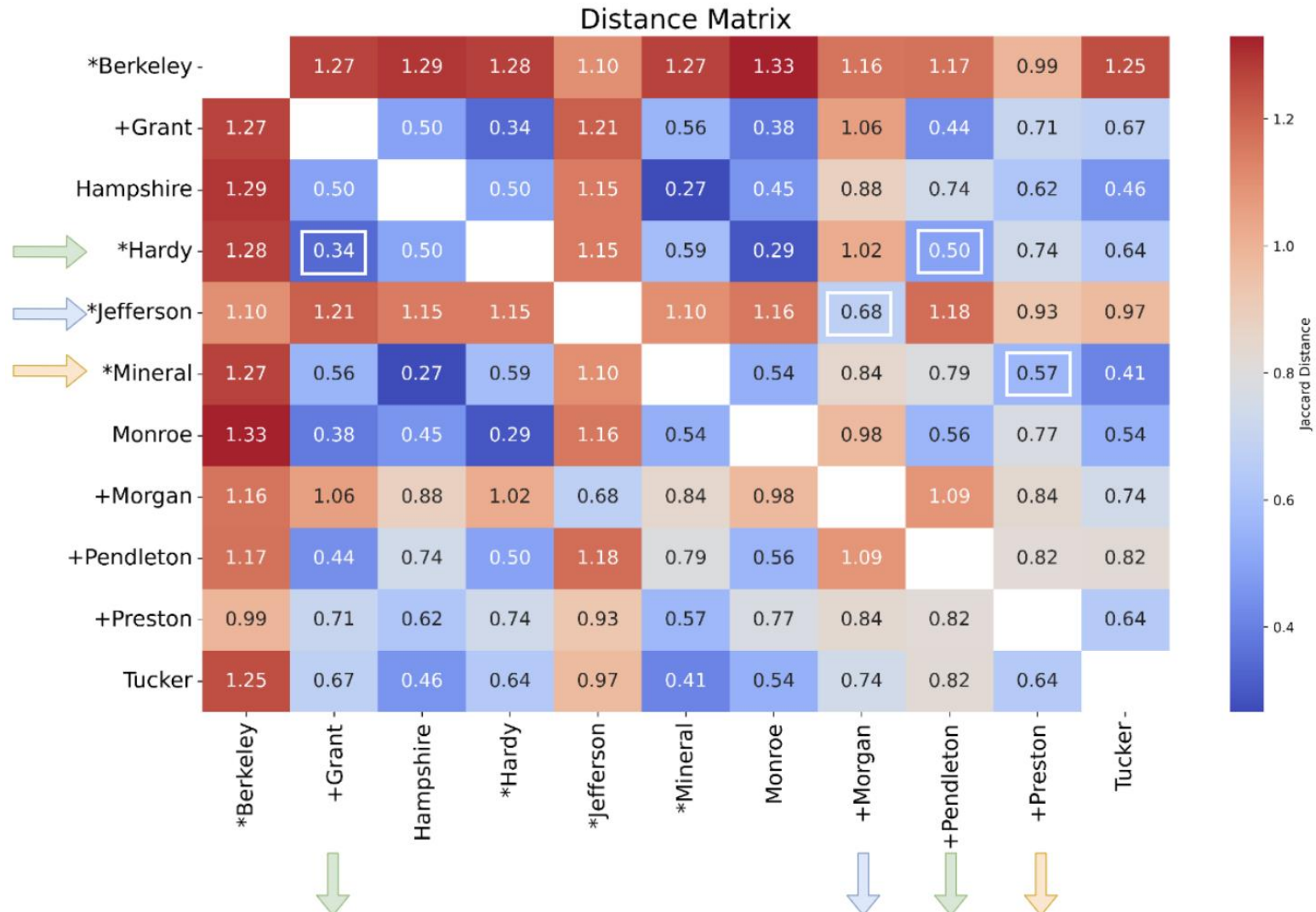
- **Efficiency:** Reduces the need to start from scratch for every new scenario.
- **Consistency:** Maintains the quality of solutions across different scenarios.
- **Scalability:** Easily applied to multiple new scenarios or regions.

# ***Applying Transfer Learning to BMPs***

- Select New Counties (Scenarios):
  - Identify new areas where BMPs need to be implemented.
- Similarity Measure:
  - Use a measure (e.g., geographic, demographic, or environmental data) to determine how similar these new counties are to previously analyzed ones (Jaccard distance over the load-sources of all LRS's of a county).
- Transfer BMPs:
  - Apply the selected BMP list from similar, previously analyzed counties to the new ones.

# Transfer Learning to Other Counties

Innovative Transfer Learning for Water Quality Optimization





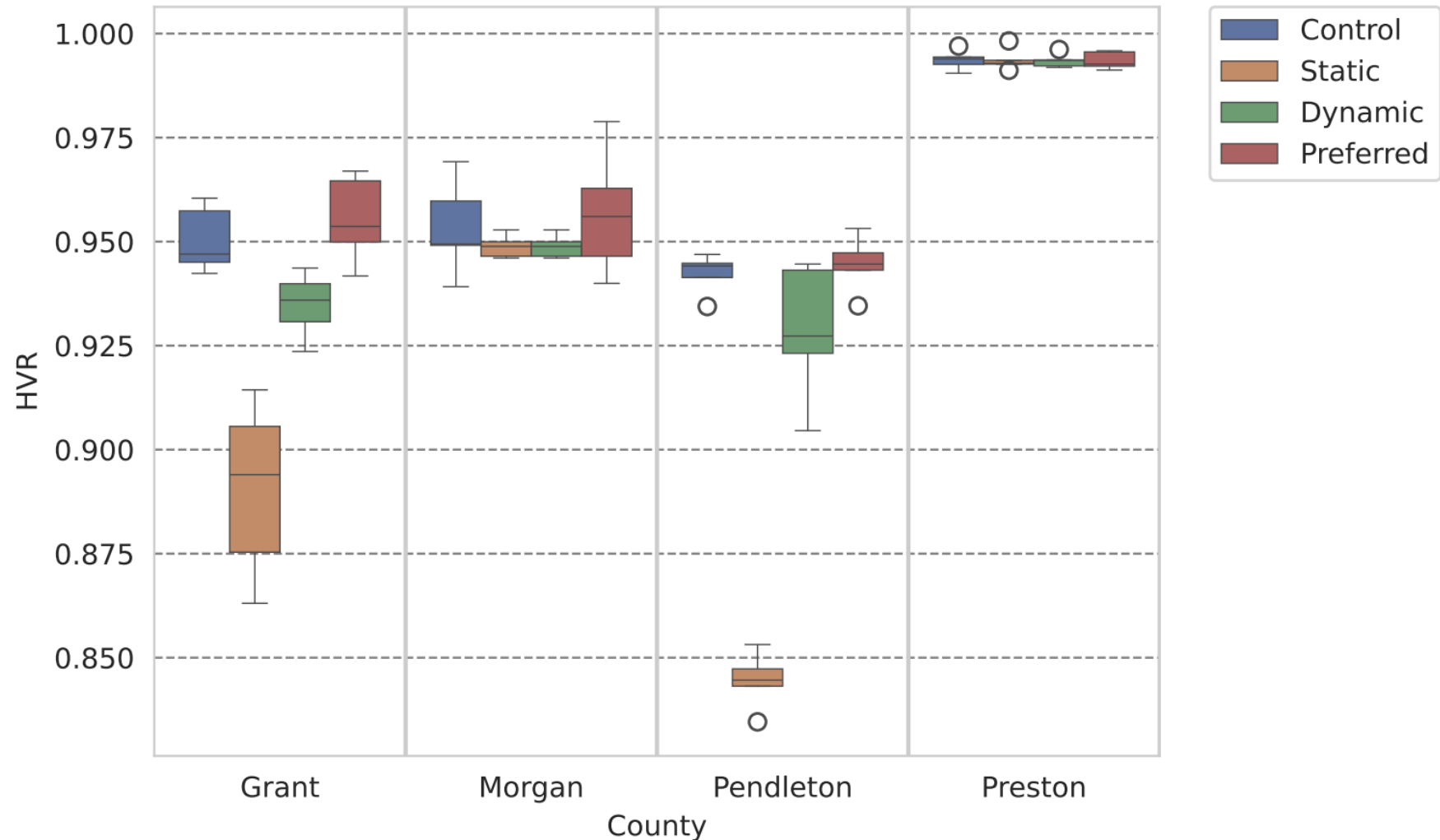
# *Transfer Learning to Other Counties*

|                  | <b>Control</b> | <b>Static (% reduction)</b> | <b>Dynamic (% reduction)</b> | <b>Preferred (% reduction)</b> |
|------------------|----------------|-----------------------------|------------------------------|--------------------------------|
| <b>Grant</b>     | 25,228         | 962 (3.8%)                  | 1217 (4.8%)                  | 8,036 (31%)                    |
| <b>Morgan</b>    | 11,880         | 466 (3.9%)                  | 466 (3.9%)                   | 3,947 (33%)                    |
| <b>Pendleton</b> | 33,083         | 1,207 (3.6%)                | 1,851 (5.6%)                 | 10,483 (31%)                   |
| <b>Preston</b>   | 1,470          | 53 (3.5%)                   | 118 (8%)                     | 447 (30%)                      |

Above counties were not seen by the innovization study, but the right identification of BMPs could be successfully transferred.

# *Transfer Learning to Other Counties*

Innovative Transfer Learning for Water Quality Optimization

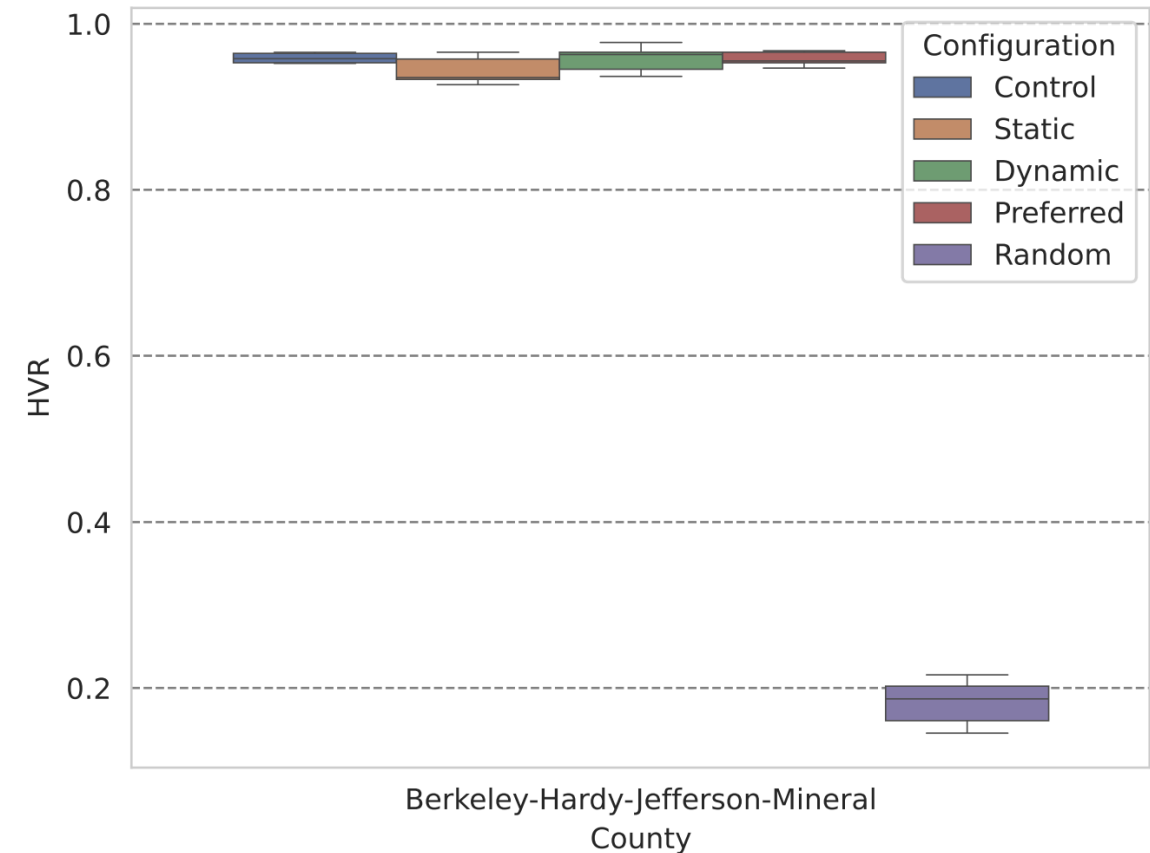


# *Transfer Learning (Multi-county)*

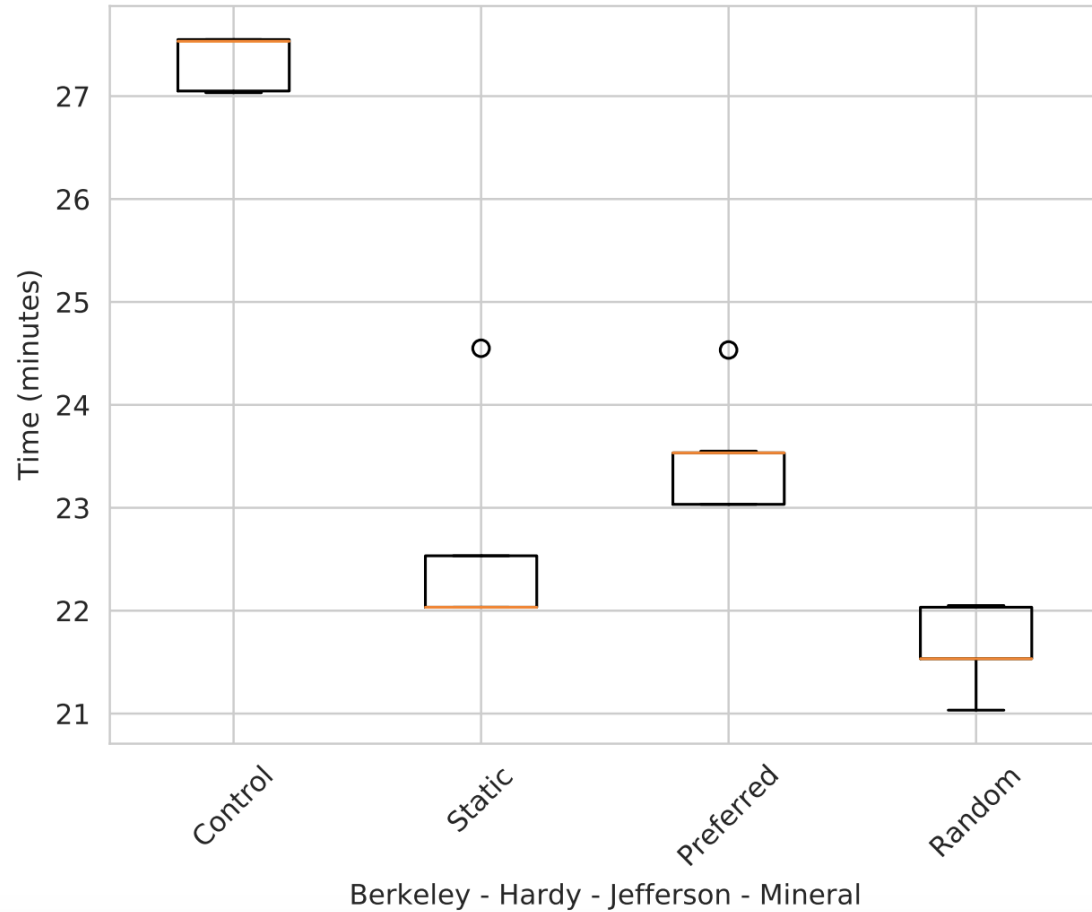
| Re-optimization | # Variables |
|-----------------|-------------|
| Control         | 65,260      |
| Static          | 2,456       |
| Dynamic         | 5,882       |
| Preferred       | 2,456       |

The random approach could not converge in a multi-county scenario when BMPs were selected at random.

Even when the number of variables increased, re-optimizing with the selected BMPs produced a competitive result.



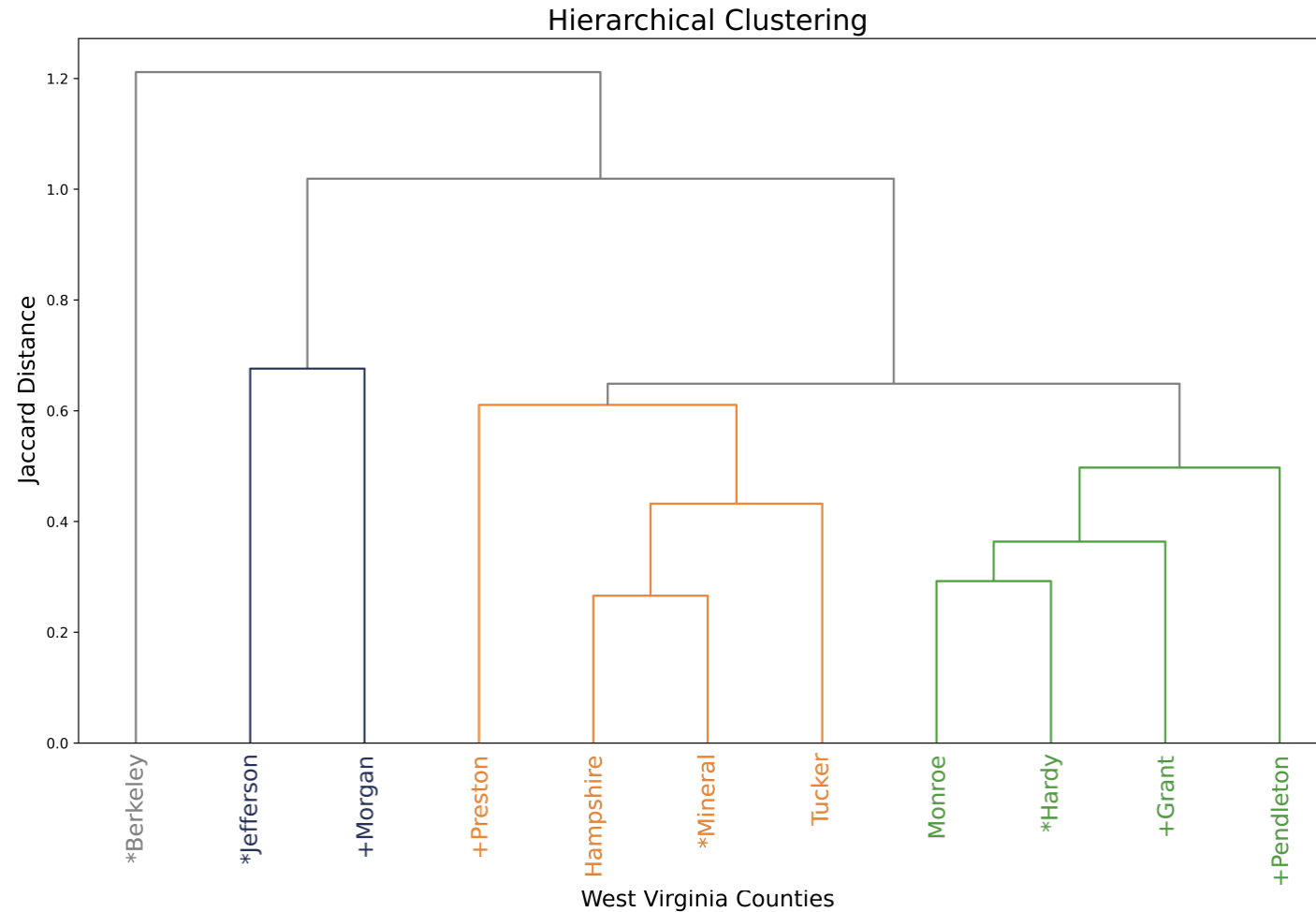
# *Transfer Learning (Multi-county)*



- Our study suggests:
- Preferred strategy is a good compromise

# *Transfer Learning to Other Counties*

Innovative Transfer Learning for Water Quality Optimization



# Conclusions / Future work

- **Real-world** large-scale application with dozens of potential users (**reduce pollutants**).
- "Innovization" helps to perform a **comput. efficient search**.
- Re-optimization validated the use of reduced variables
- Transfer learning allowed a reduced BMP list obtained from a few counties to apply to a few more similar counties.
- Transfer learning reduces time, and complexity and shows promise to solve large-scale problems.



# iEMSs 2024 Biennial Conference: Abstracts

1. Toscano, G. A. P. Nejadhashemi, K. Deb, H. Razavi. L. Linker, 2024. Advancing Watershed Management: A Multiobjective Optimization and Multicriteria Decision-Making Platform.
2. Deb, K., Lu, Z., Kropp, I., Hernandez-Suarez, S., Hussein, R., Miller, S. and Nejadhashemi, A. P., 2024, Reliable Decision-making Under Uncertainty in Hierarchical Multi-Criterion Problems.
3. Deb, K., Goodman, E., and Chikumbo, O. 2024, Multi-objective Land Use Management and Decision-making.
4. H. Razavi. A. P. Nejadhashemi, K. Deb, Toscano, G. L. Linker, 2024. Water Resources Management: A Comprehensive Analysis of Elements, Interconnections, and Emerging Synergies.
5. H. Razavi. , G. L. Toscano, A. P. Nejadhashemi, K. Deb, Linker, 2024. Innovative Ranking Methods for Parameter Size Reduction in Large Scale Multi-Objective Optimization Problem.

# Journal Papers

- A. P. Nejadhashemi, K. Deb, G. Toscano, H. Razavi, L. Linker. Leveraging Innovization and Transfer Learning to Optimize Best Management Practices in Large-Scale Watershed Management. Journal of Environmental Modelling & Software. Accepted with minor revisions.

# NEXT STEPS

- Scale up to watershed level optimization
- Parallel computing platform for even faster execution
- Workshops with CBP users for feedback and improvement of our approaches

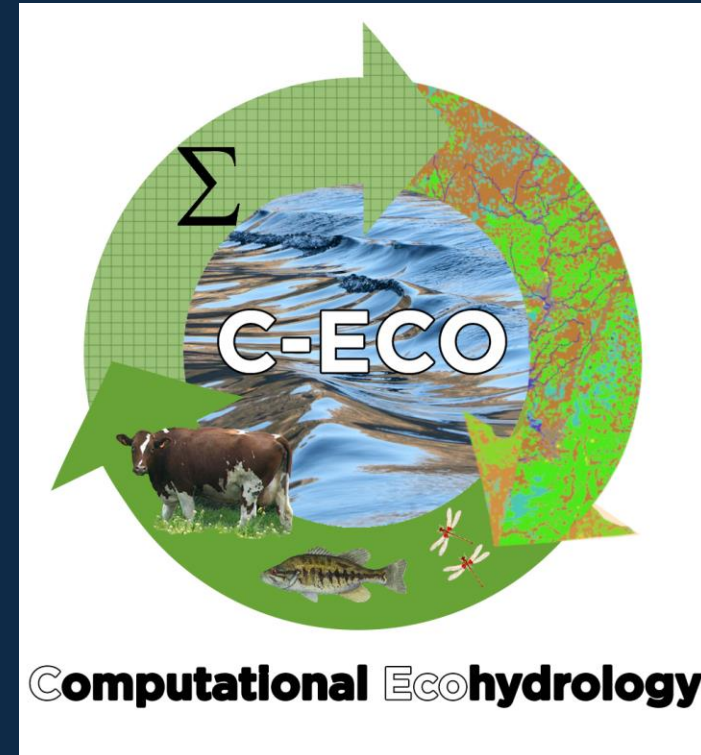


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Computational Optimization and Innovation

Thankyou





Thank you!